



NORWEGIAN MAPPING
AUTHORITY

Campaign and vectors, geoid and leveling. Combined adjustment

SPATIAL DATA – FOR BENEFIT OF THE SOCIETY

Olav Vestøl, Torbjørn Nørbech, Oddvar Tangen

Background

NN2000, our new height system for gravity related heights

- Only 23 % of the points in our reference network (Stamnett and Landsnett) are levelled
- For points not levelled NN2000 heights will be derived from ellipsoidal heights and a fitted geoid model (height reference model)
- **The accuracy of the NN2000-heights on these points in our reference network depends on the accuracy of the ellipsoidal heights.**
- All available observations, vector as well as campaigns, should be used.



DEFINITION OF TERMS

Frequently used in this presentation

- Campaign measurement
 - After processing the result is coordinates
 - Many points processed at a time
 - Usually several days of observation times
 - Advanced academic university software (Gipsy, Bernese, Gamit)
- Vector measurement
 - After processing the result is coordinate differences (vectors)
 - Usually only one vector is processed at a time
 - Usually only hours of observation time
 - Commercial software (GPPS, GeoLab, LineComp, SKI ...)



CAMPAIGN MEASUREMENTS

A part of the IGS05-project

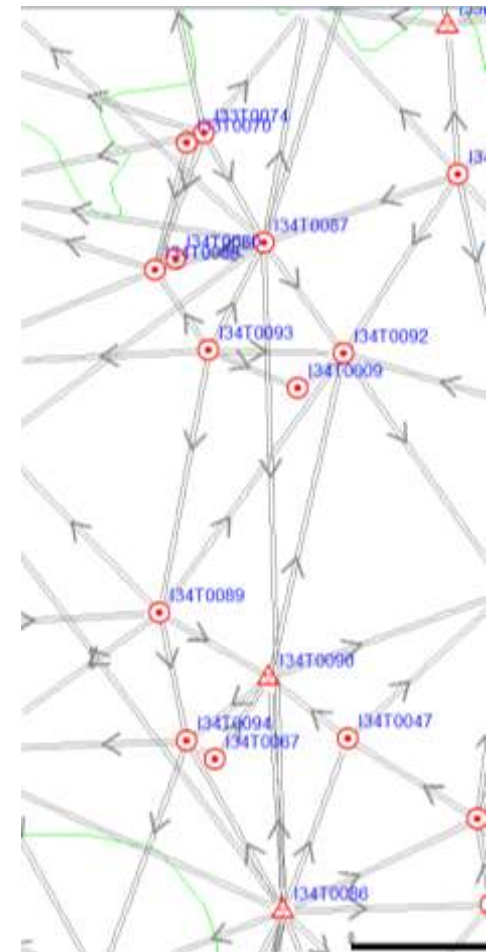
- 5 – 7 days of measuring
- Processed by use of Bernese GPS-software
- Constrained to the Norwegian permanent stations
 - Epoch: 31th of July 2009
 - Coordinated based on daily solution back to 2000
- Measured in 2009 and 2010
- Spatial distribution of 30 km



VECTOR MEASUREMENTS

In the first and second order reference network. (Stamnett and Landsnett)

- Observed from 1994 – 2009
- Processed in the year of observation by use of different commercial software
- Length from 3 – 20 km
- About 90% measured and processed by Norwegian Mapping Authorities
 - About 10% from external organisations
- Used in the calculation of the our reference network



HOW TO COMBINE

Vector- and campaign measurement

- Calculation of ellipsoidal heights H_{ell} and height differences dH_{ell}
 - H_{ell} from campaigns. The co-variances must be derived from the 3D-file.
 - dH_{ell} from vectors.

- Corrections
 - IGS05-N
 - Correct the vectors for land uplift
 - EUREF89 (ETRS-89)
 - Correct the campaigns for land uplift
 - Unknown offset between the datum

- Variance component estimation
 - Weight model for the vectors
 - Weight model for the campaigns



VARIANCE COMPONENT ESTIMATION

For the ellipsoidal height difference in the vectors

The method of Olav Mathisen (Based on least square adjustment)

$$C = C_0 + k_1 C_1 + k_2 C_2 + k_3 C_3 + \dots$$

where

$$C_1 = I, \quad C_2 = \begin{bmatrix} d_1^2 & & & \\ & d_2^2 & & \\ & & d_3^2 & \\ & & & \dots \end{bmatrix} \quad \text{og} \quad C_3 = \begin{bmatrix} dh_1^2 & & & \\ & dh_2^2 & & \\ & & dh_3^2 & \\ & & & \dots \end{bmatrix}$$

Giving as a middle

$$C = 1.0 \text{cm}^2 + 0.1 \text{cm}^2 D_{km}^2 + 2.5 \text{cm}^2 dH_{km}^2$$



VARIANCE COMPONENT ESTIMATION

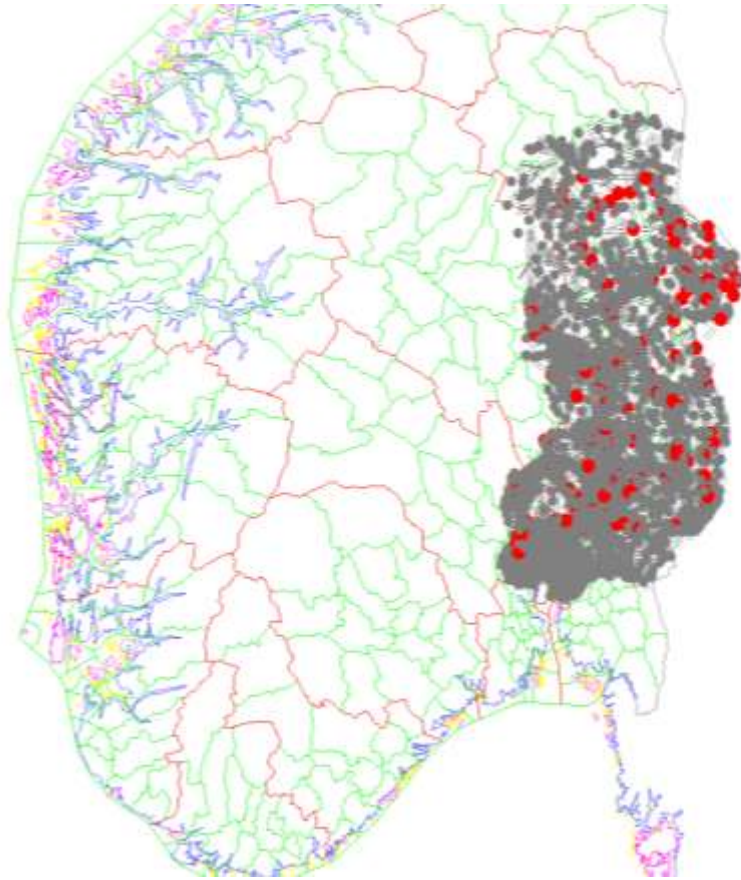
For campaign measurement

- “Simplified estimator” by Caspary 1988
 - Call the campaigns one group of observations and the vectors an other group
 - Calculate the sum of redundancy for each group. (1)
 - Calculate the weighted sum of squared residuals for each group (2)
 - Calculate the a posteriori variance of unit weight for each group by dividing (2) by (1).
 - Iterate the adjustment and redefine the unit weight observation until a posteriori variance is unity for both groups.
- Result
 - **The Bernese variances must be multiplied by more than 100.**
 - Using 100 gives in average a standard deviation of 9 mm in Hedmark and 4 mm in Rogaland



REFERENCE NETWORK HEDEMARK

Campaign points in red.

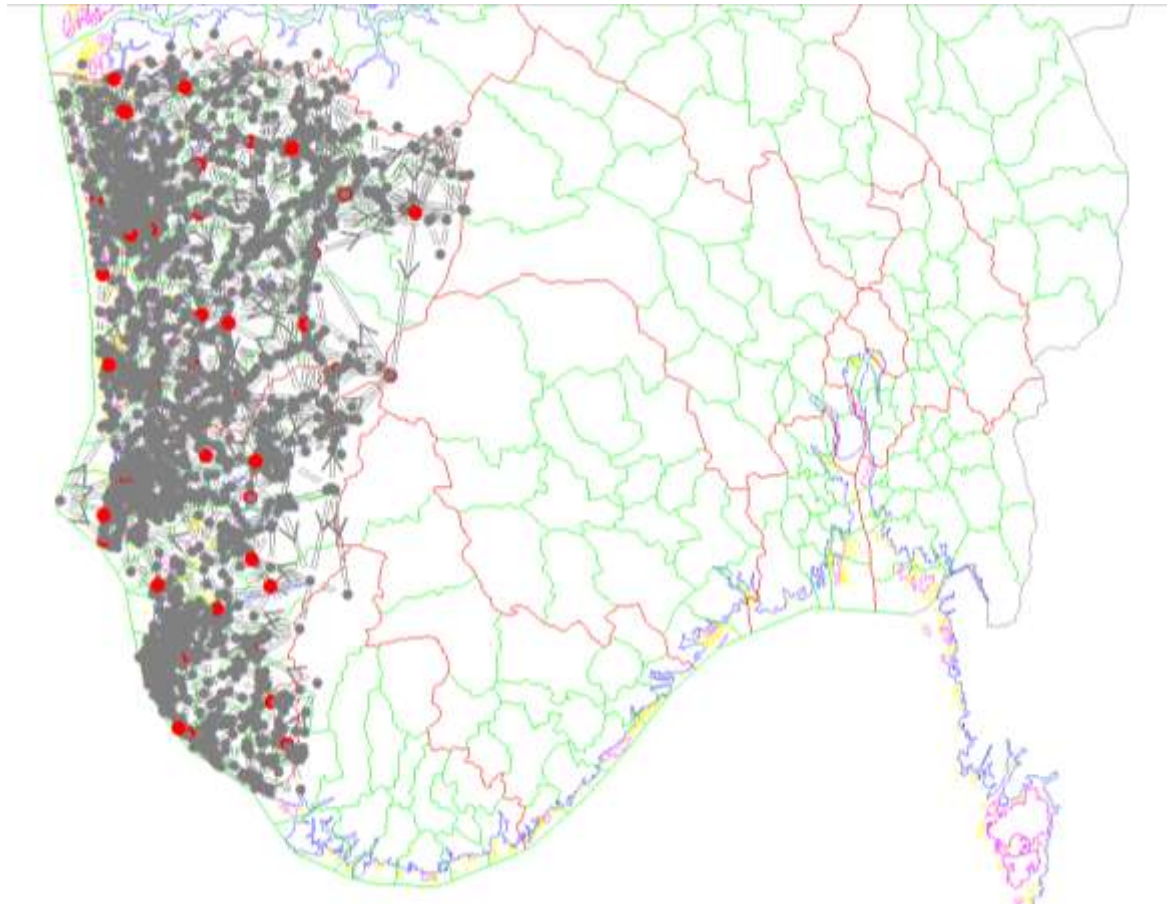


- 131 campaigns
- 8506 vectors
- 2640 points



REFERENCE NETWORK ROGALAND

Campaign points in red.



- 44 campaigns
- 6325 vectors
- 2047 points



CAMPAIGN HEIGHTS VERSUS VECTOR HEIGHTS

Global test

Rogaland	
Point	Deviation
B36T0200	0,035
A32T0425	0,019
B36T0608	0,019
B39T0175	-0,015
C38T0434	-0,023
A33T0192	0,014
A37T0017	-0,023
B35T0620	0,012
B36T0589	-0,009
C36T0245	0,011

Hedmark	
Point	Deviation
H31T0244	0,057
I31N0100	-0,063
G34T0751	0,020
G35T1298	0,023
I31N0111	-0,029
H30N0019	0,032
H30N0009	0,033
I33N0069	0,027
H33T0466	-0,019
H29T0187	-0,020
H35T0238	0,017

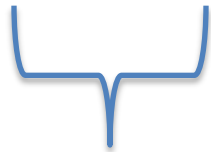


COMBINED ADJUSTMENT OF NN2000-HEIGHTS

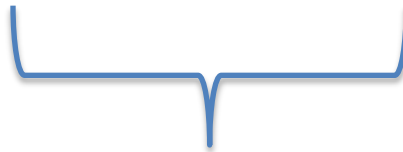
Observation equations

For vectors

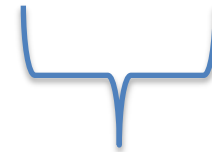
$$dh_{ell} + n = (H_2 - H_1) + (\text{mod}_2 - \text{mod}_1) + (s_2 - s_1)$$



NN2000
heights



Geoid heights from
NKG2004



Unknown
signals

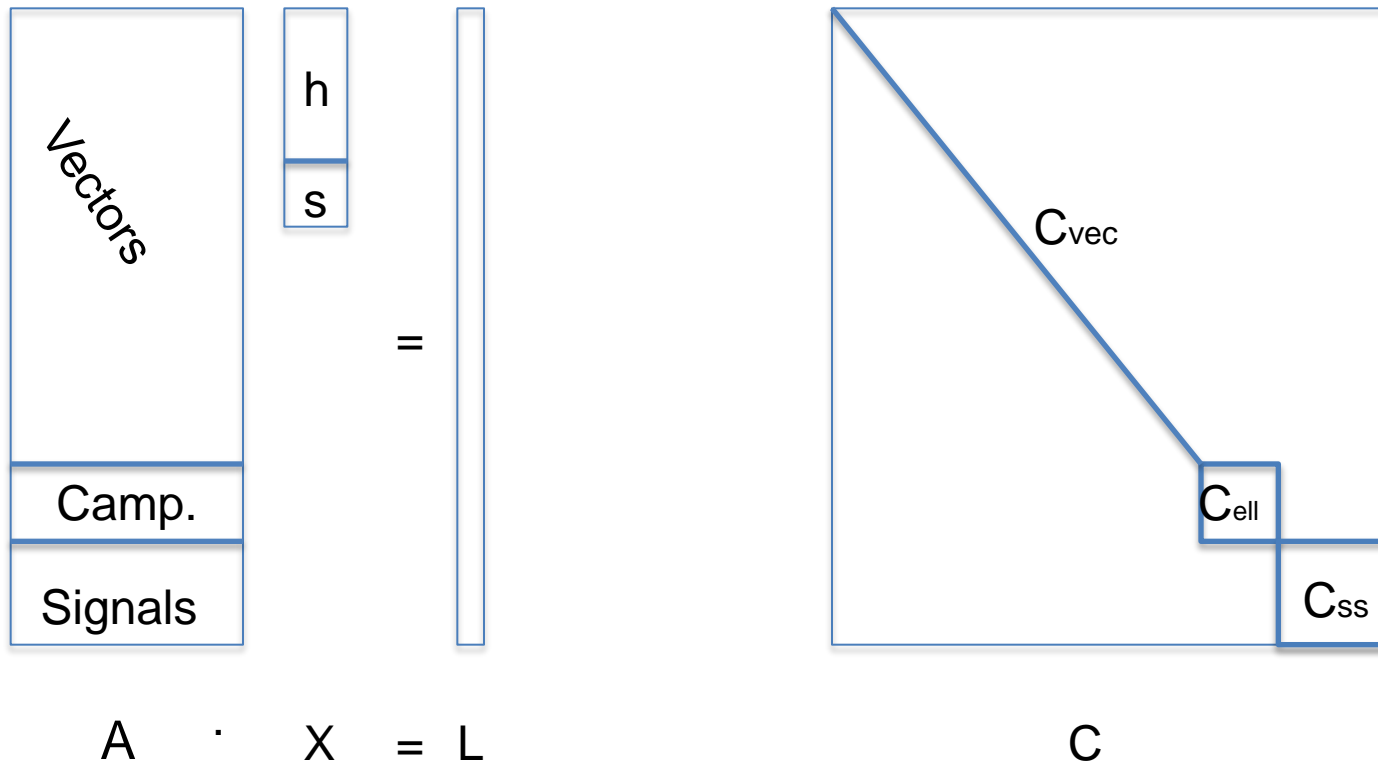
For campaigns

$$h_{ell} + n = H + \text{mod} + s$$



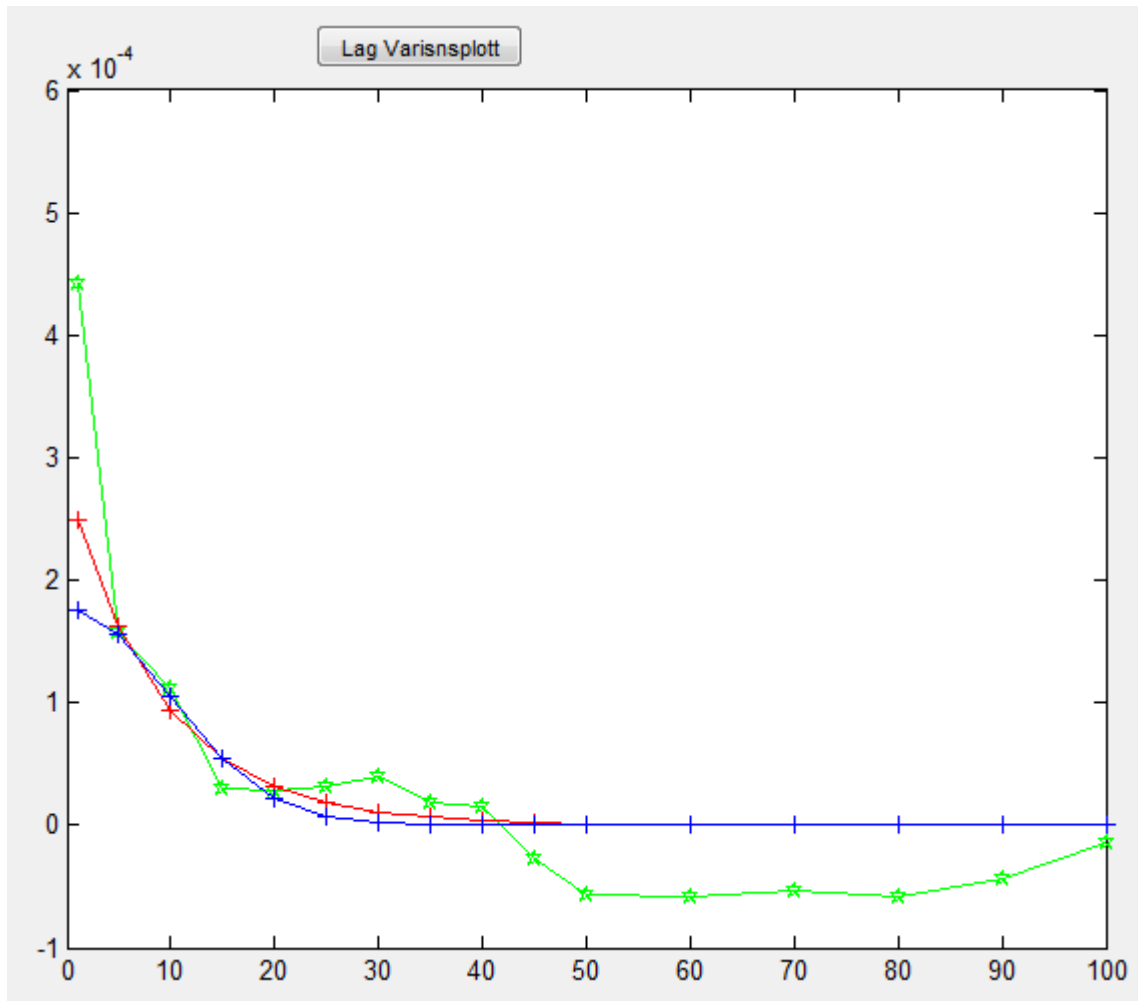
COMBINED ADJUSTMENT. NN2000 HEIGHTS KNOWN

Schwartz method



VARIANCE PLOT FOR HEDMARK

Based on residuals: Geoid model ÷ (ellipsoidal height ÷ normal height)

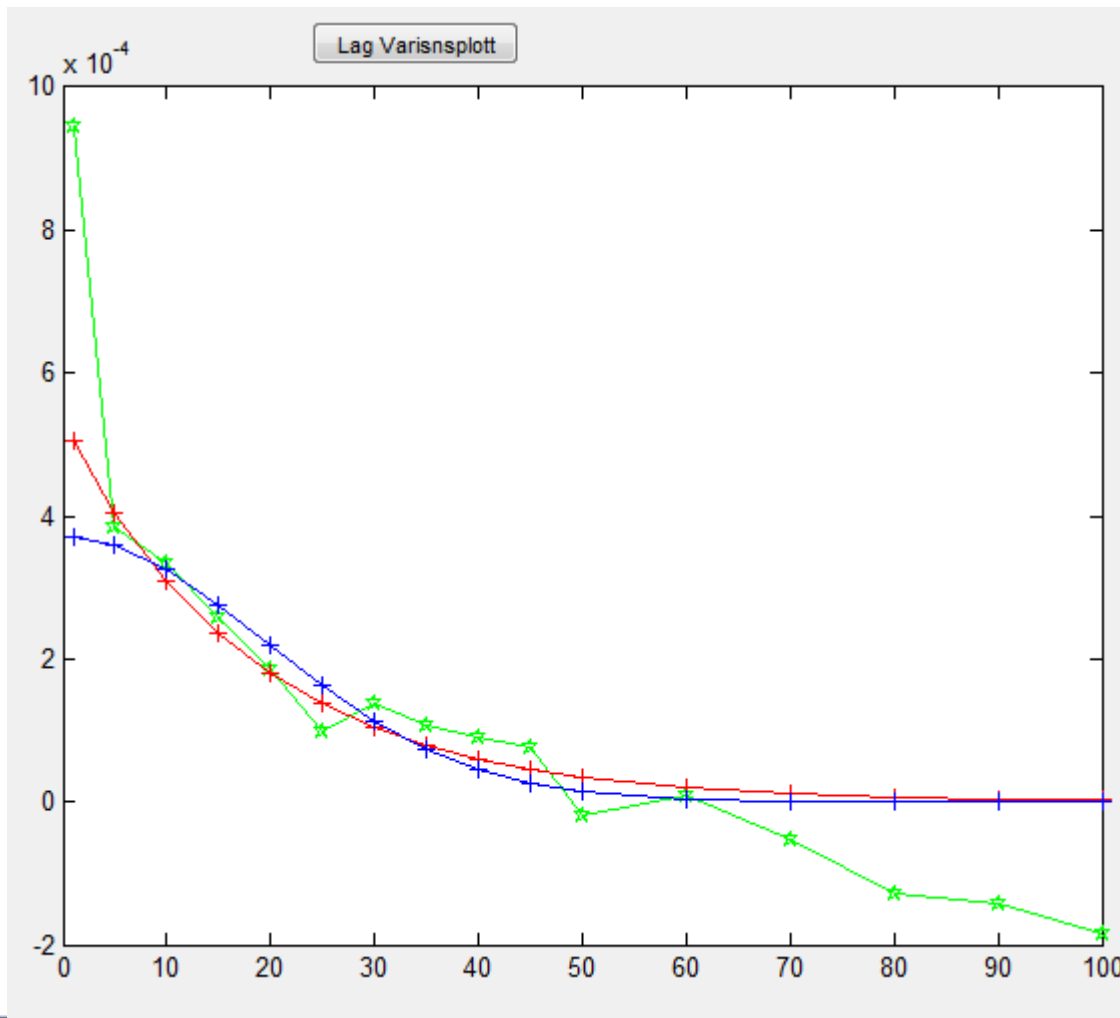


- Observed
- $\sigma^2 e^{-\beta D}$
- $\sigma^2 e^{-\beta D^2}$



VARIANCE PLOT FOR ROGALAND

Based on residuals: Geoid model ÷ (ellipsoidal height ÷ normal height)

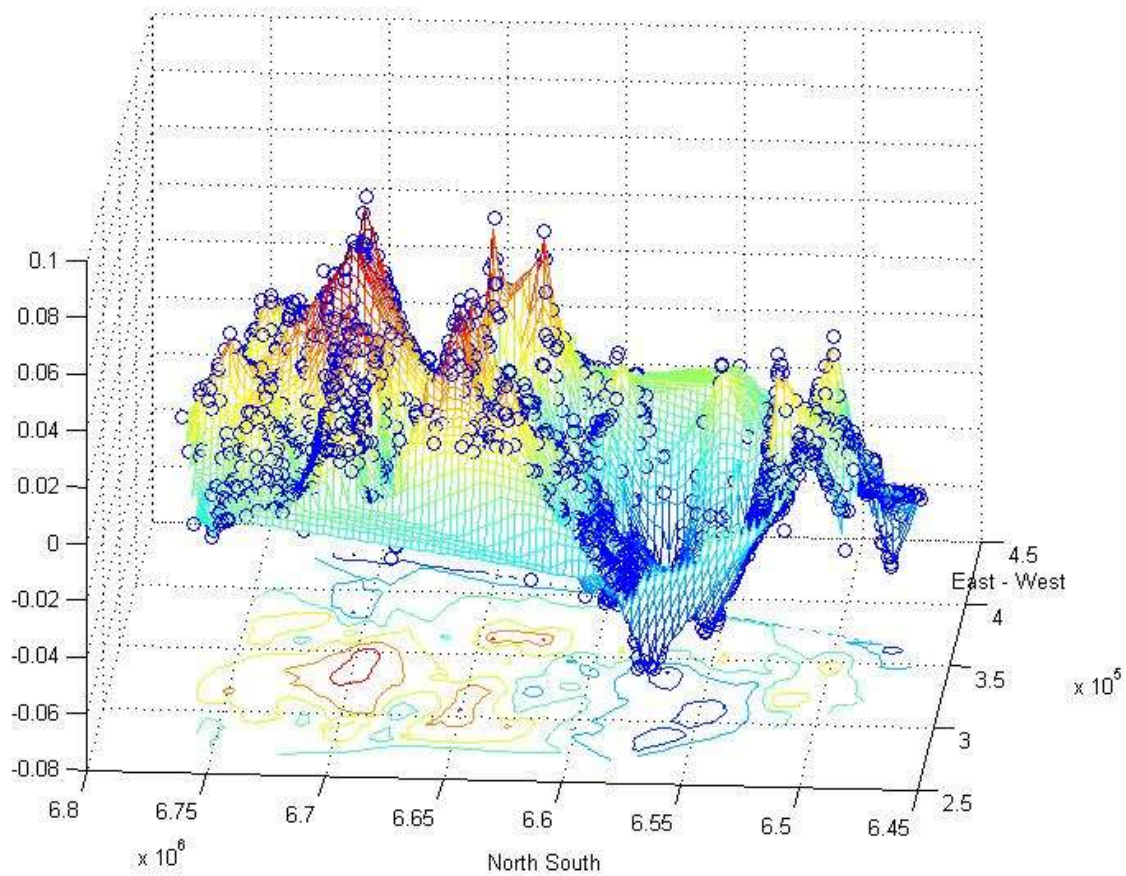


- Observed
- $\sigma^2 e^{-\beta D}$
- $\sigma^2 e^{-\beta D^2}$



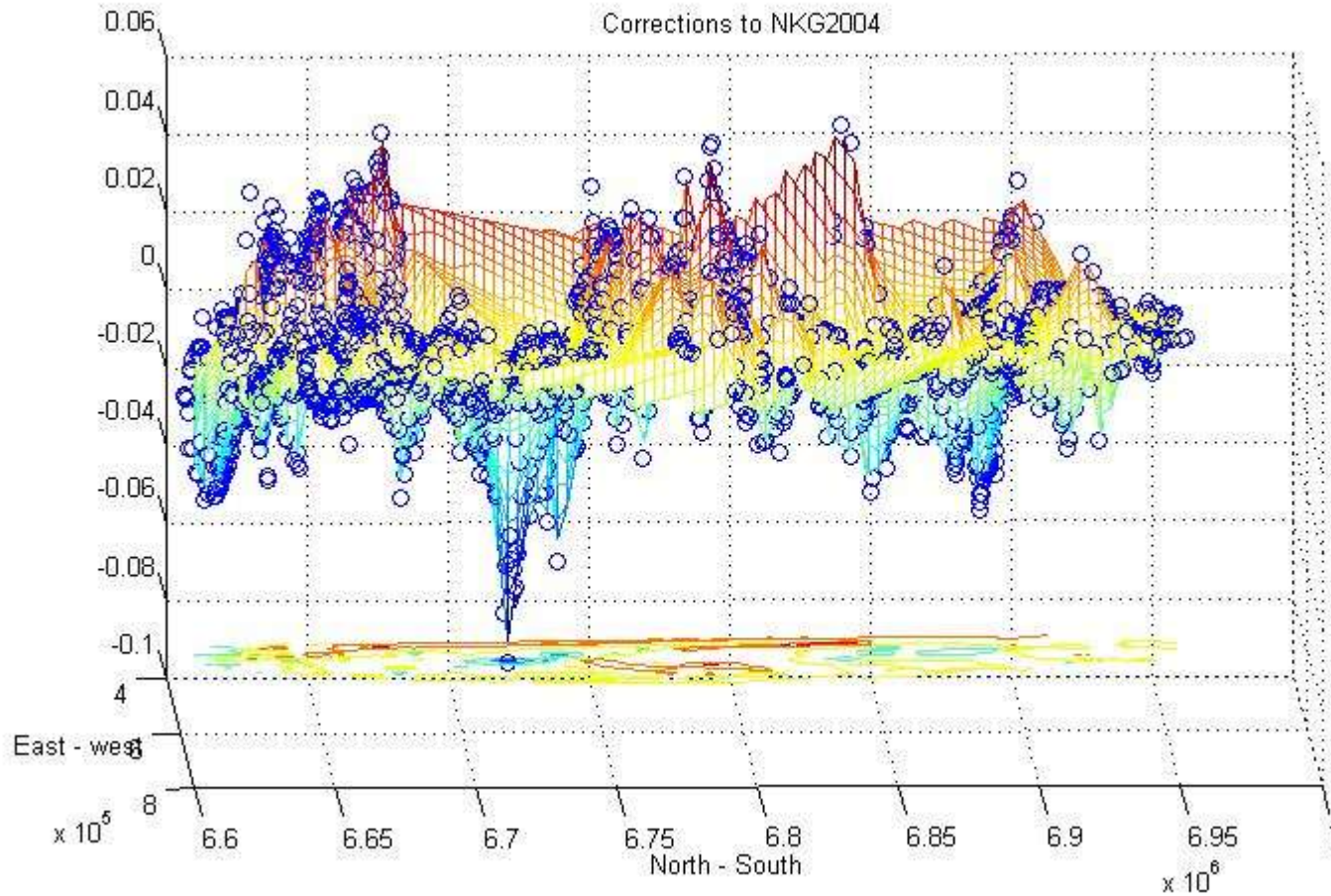
SIGNALS

Rogaland



SIGNALS

Hedmark



LEVELLING CHECK ROGALAND

What fits best to the levelling net?

Point	Camp - Vectors	Camp - Levelling	Vectors - Levelling	T-value	Remark
B36T0200	0,035	0,038	0,003	9,3	Dynamited close by
A32T0425	0,019	0,004	-0,015	0,8	17 vectors in 4 setups
B36T0608	0,019	0,025	0,006	5,8	20 vectors in 4 setups
B39T0175	-0,015	-0,074	-0,063	17,0	4 cm diff forward and backward
C38T0434	-0,023	0,000	0,023	0,3	8 vectors in 2 setups
A33T0192	0,013	0,005	-0,008	0,1	
A37T0017	-0,023	0,021	0,042	5,3	Incorrect levelling?
B35T0620	0,012	0,002	-0,010	0,6	21 vectors and 3 setups
B36T0589	-0,009	0,012	0,021	3,4	34 vectors in 7 setups
C36T0245	0,011	-0,004	-0,015	0,1	15 vectors in at least 4 setups



LEVELLING CHECK HEDMARK

What fits best to the levelling net?

Point	Camp - Vectors	Camp - Levelling	Vectors - Levelling	T- value	Remark
H31T0244	0,057	0,004	-0,061	0,0	Lev. and campaign unreliable.
I31N0100	-0,063	-0,036	0,027	1,1	Unstable stone?
G34T0751	0,020	-0,001	0,021	0,2	40 vectors in at least 11 setups
G35T1298	0,023	0,019	-0,004	1,8	40 vectors in at least 3 setups
I31N0111	-0,029	0,012	0,041	1,1	6 vectors in 2 setups
H30N0019	0,032	0,001	-0,031	0,1	5 vectors in 2 setups
H30N0009	0,033	0,026	-0,007	0,1	5 vectors in 1 setup
I33N0069	0,027	0,008	-0,019	0,6	5 vectors in 1 setup
H29T0187	-0,020	-0,015	0,005	2,9	14 vectors in at least 3 setups
H35T0238	0,017	0,008	-0,015	0,6	8 vectors in at least 2 setups



CONCLUSIONS

Different techniques controls each other

- The network of vectors may control campaign measurement and vice versa
- NN2000-heights and geoid models may give an extra control of both vector- and campaign measurement
- Vector- and campaign measurement may reveal errors in the levelled heights



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- Thank you for your attention!