



Separation models in Norway

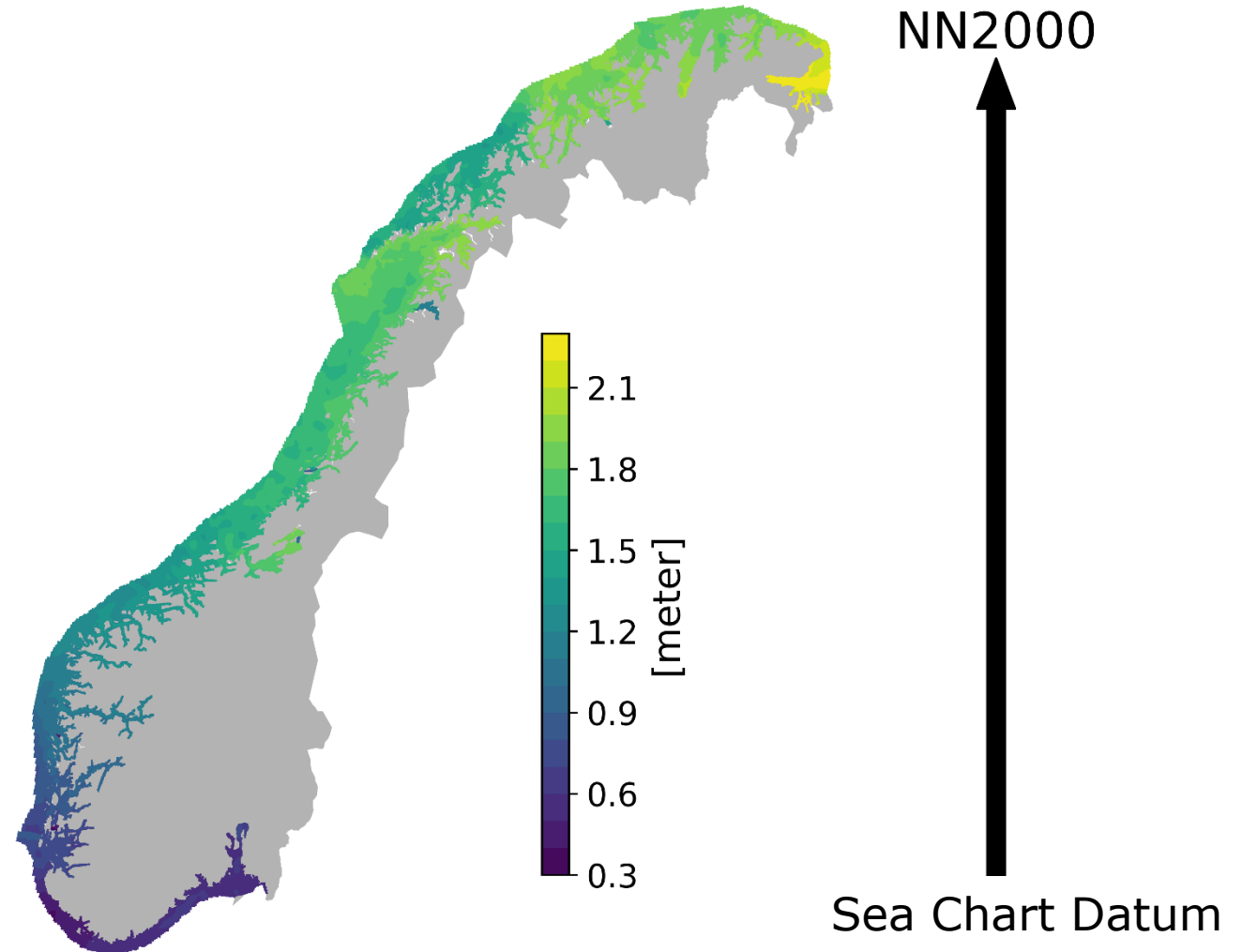
NKG General Assembly 2022 - Copenhagen

Two reference levels

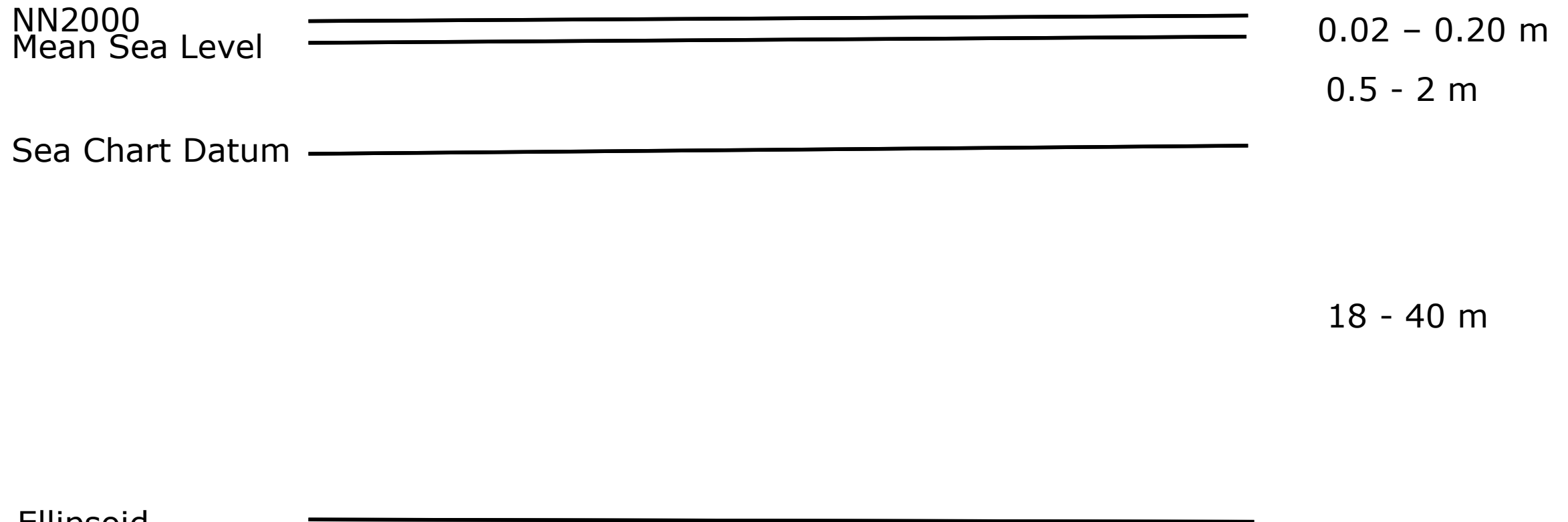
- On land: NN2000
- On sea: Sea Chart Datum =
LAT (Lowest Astronomical Tide)

- **Make a model of the difference!**

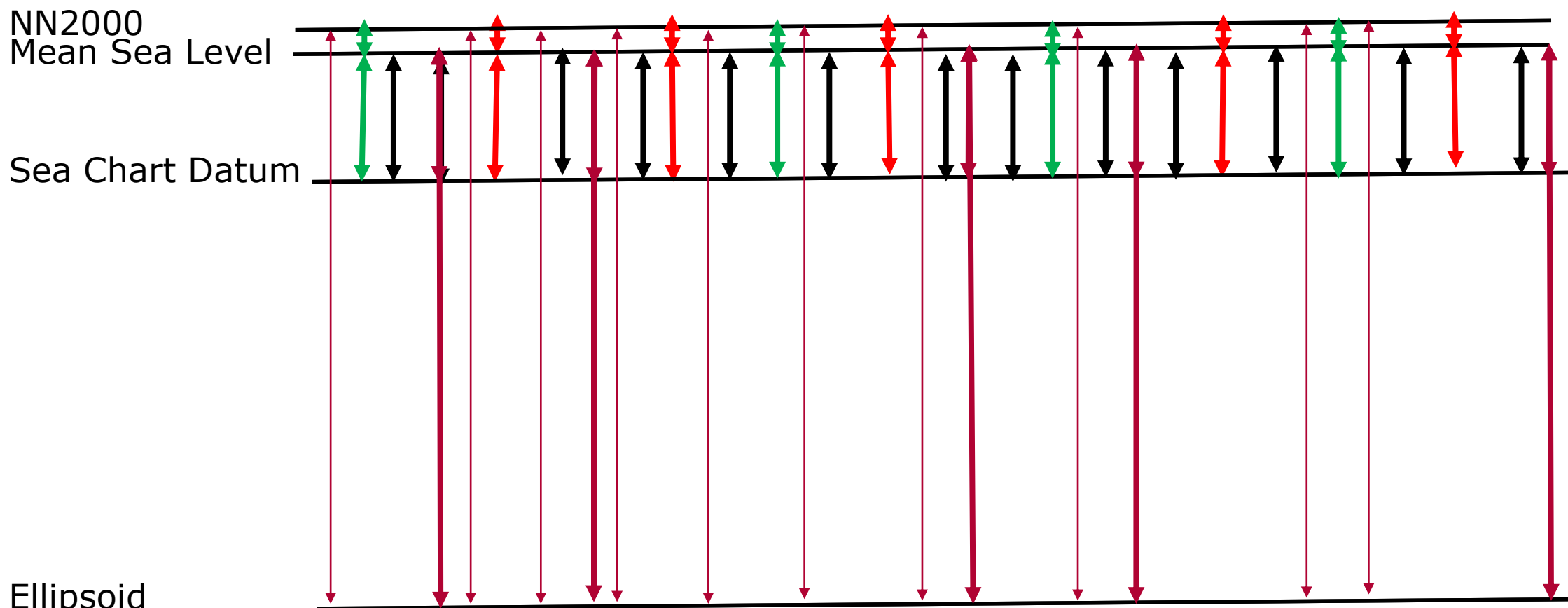
Problem:
We have few direct
observation of this
difference



Other relevant reference levels

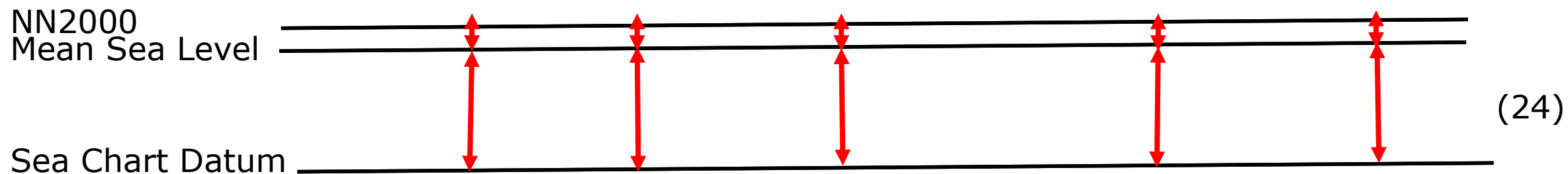


Observations of distances between reference levels



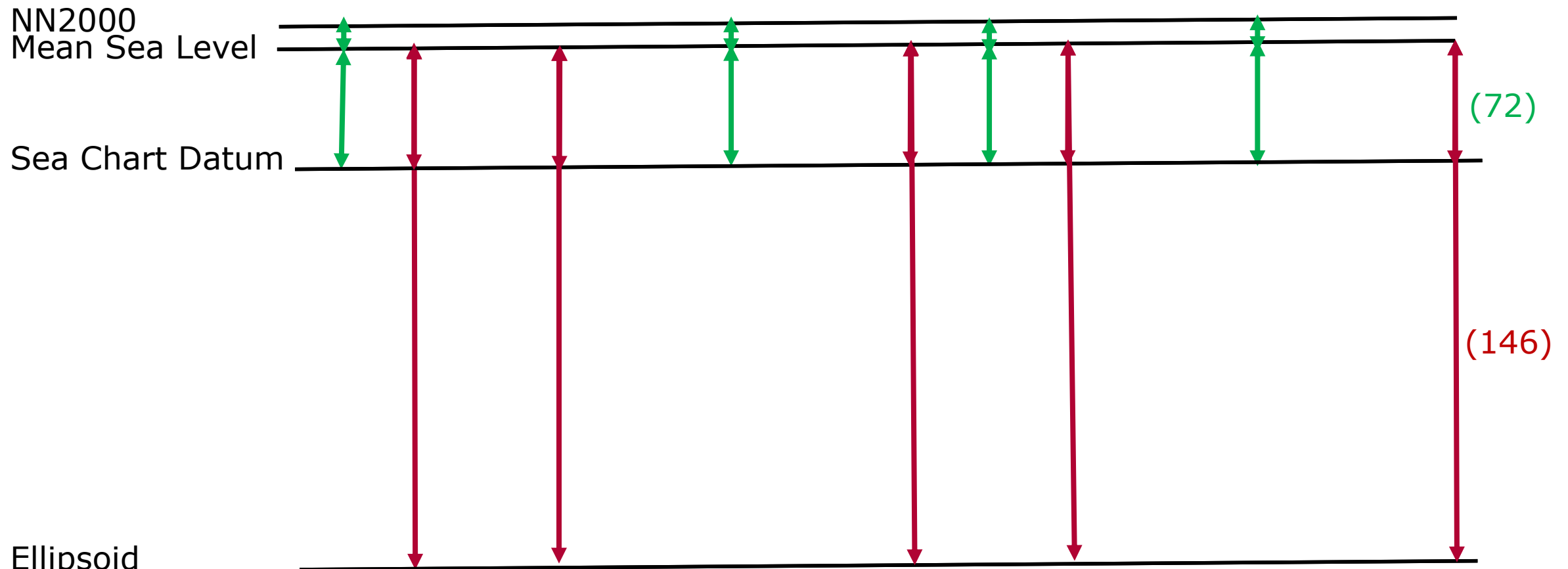
Ellipsoid

Permanent tide gauges



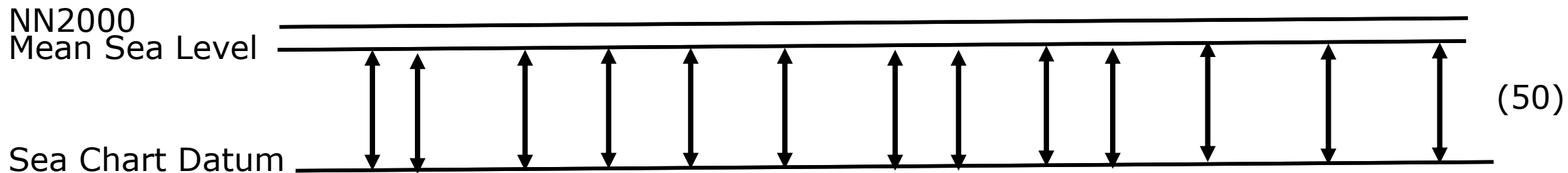
Ellipsoid

Temporary tide gauges

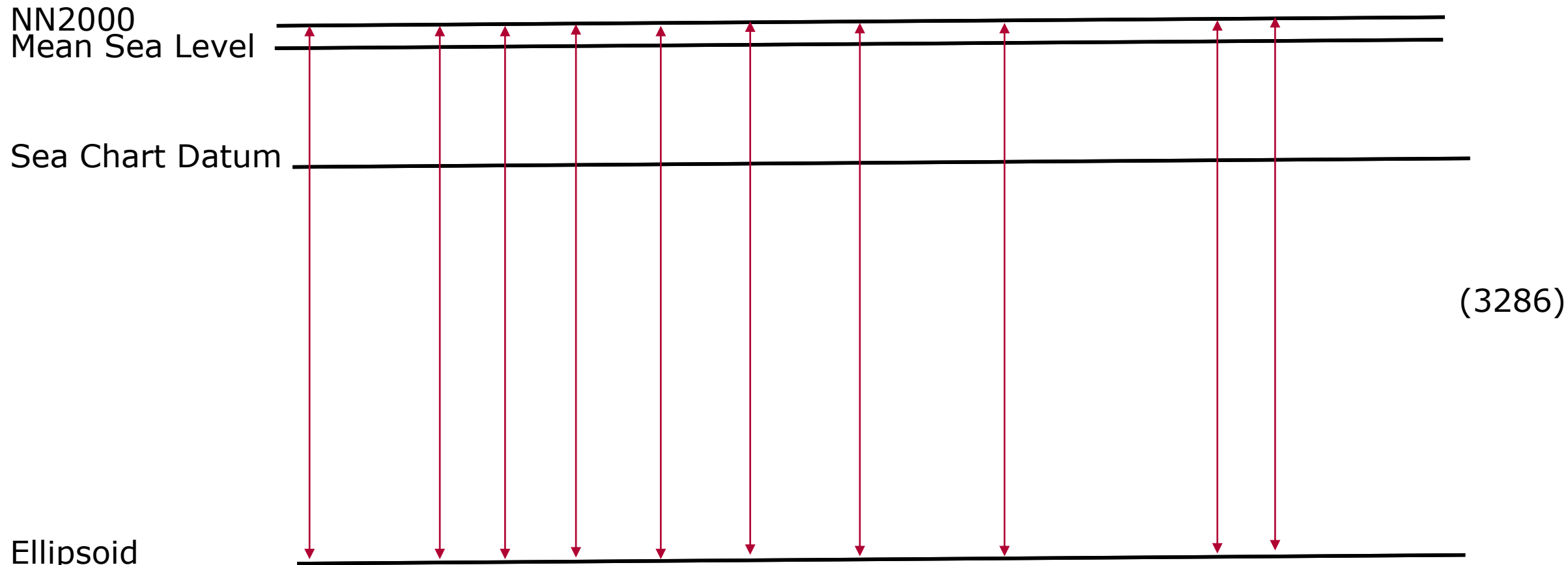


Ellipsoid

Temporary tide gauges, not connected to any benchmark



GNSS/levelling points



Ellipsoid

Strategy

NN2000
Mean Sea Level



Sea Chart Datum



"MDT"
Z0-model

Make three models:

1. NN2000 above Mean Sea Level ("MDT")
2. NN2000 above the ellipsoid ("Href-model")
3. Mean sea level above Sea Chart Datum ("Z0-model")

Start two processes. First, we calculate model 1 and 2, then model 3 in a separate process

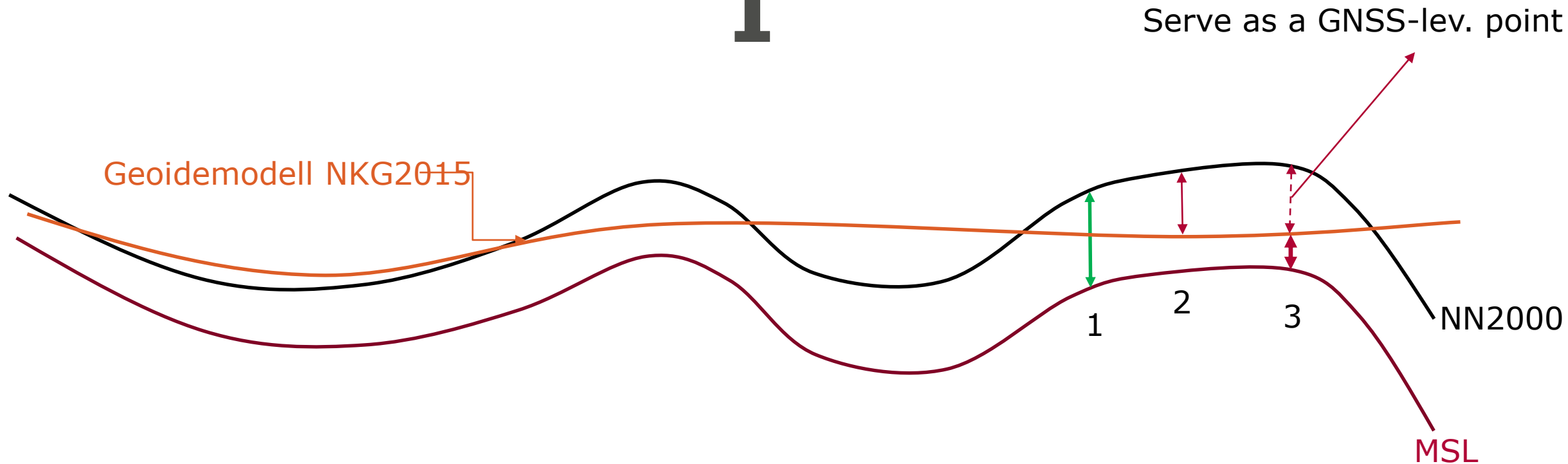
Href

Ellipsoid



The first process – 'MDT' and Href

I



- 1: Tide gauge connected to levelling network
- 2: GNSS-levelling point
- 3: Tide gauge connected to the ellipsoid

The first process – 'MDT' and Href

II

- Least square collocation
- Two trend functions (calculated deterministic):
 - Distance between NN2000 and Mean Sea Level ('MDT')
 - Corrections to the gravimetric geoid model **NKG2015**
- Two set of signals (calculated stochastic):
 - Distance between NN2000 and Mean Sea Level (In addition to the trend)
 - Corrections to the gravimetric geoid model (In addition to the trend)

Some remarks on the new Href-models and NN2000

- The new Href-model enable us to improve the realizations of NN2000 far away from the levelling lines
- We know already that current realization in some regions have errors of 10 – 20 cm
- For consistency we cannot take the model in use for height determination without changing our current realization of NN2000
- However, the new Href-model is used as an internal model to make other separations models in combinations with others

The second process – the Z0-modell I

Use existing zone information as start values:

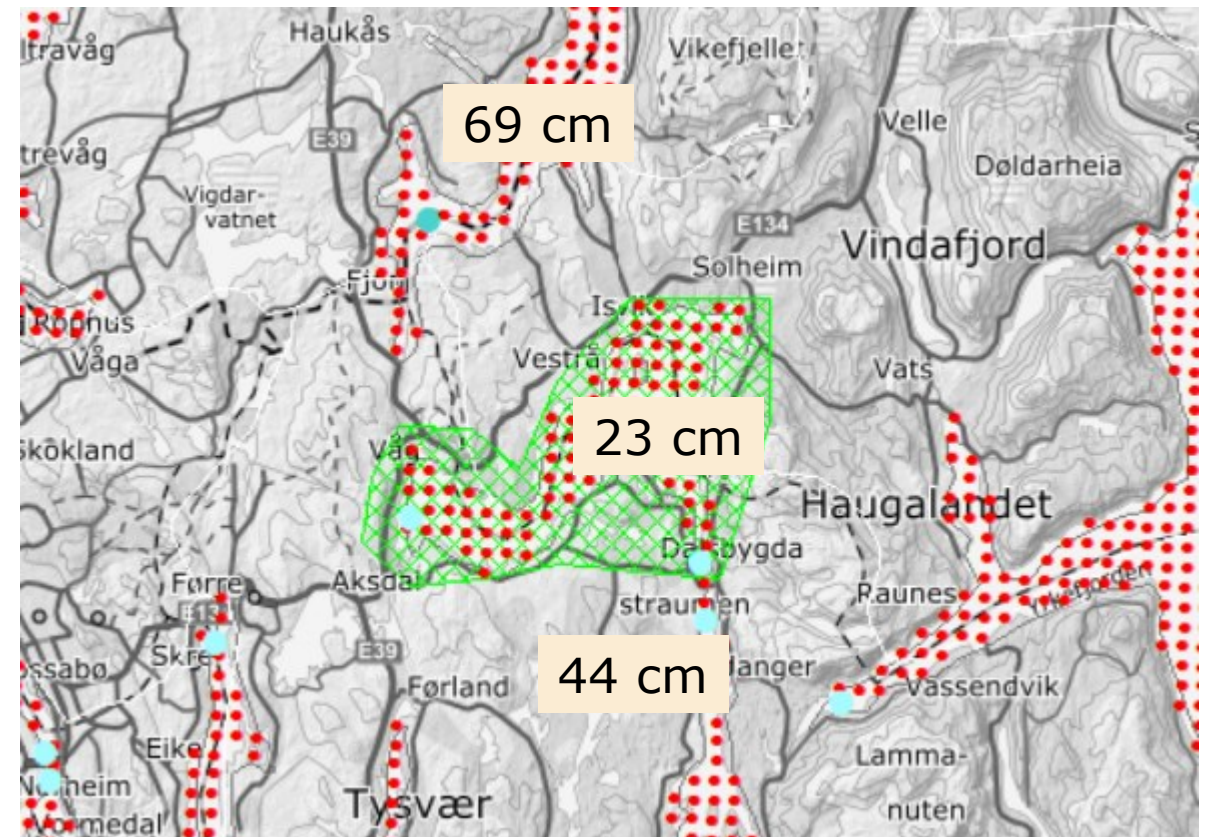
- Each zone has an individual Z0-value
- From each zone we pick the Z0-value for one or more positions.
- From these values a first model is calculated – a “zero model”

All available tide gauge observations are then used to correct this first “zero model”



The second process – the Z0-modell II

- In open sea the variation of LAT is as smooth as MSL.
- In complex fjord system, the variation can be huge over short distances.
- **A common covariance function will not work in both situations**
- Trick: Isolate fjord systems inside polygons and add 200 km to all distances to point inside the polygon.
- Use sea-distances – not the direct distance!



Combinations:

NN2000
Mean Sea Level



Sea Chart Datum



NN2000 above Sea Chart Datum = $MDT + Z0\text{-model}$
Mean Sea Level above Ellipsoid = $Href \div MDT$

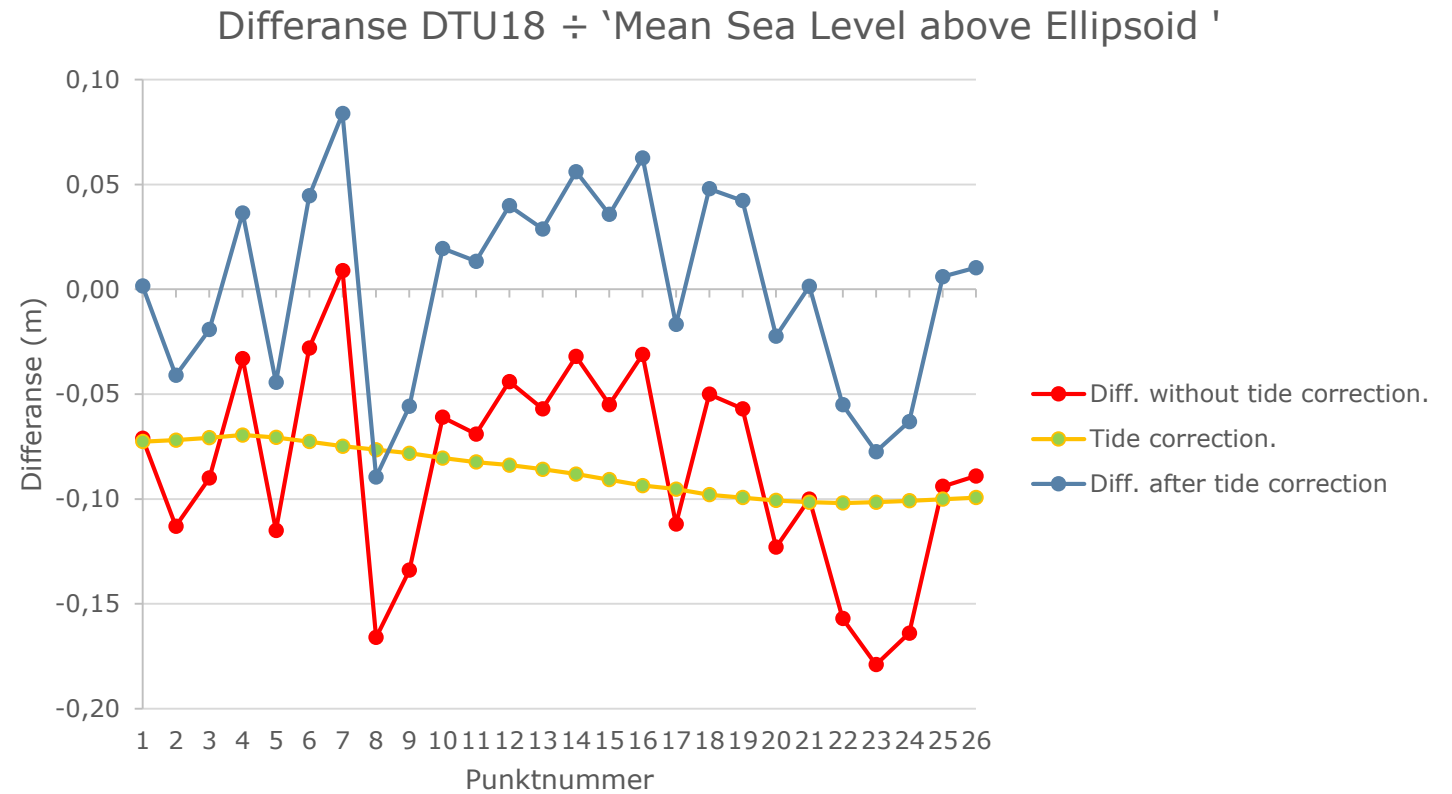
"MDT"
Z0-model

Href

Ellipsoid



Comparision with DTU18 (Danish Technical University)



Conclusions and further work

- Combination of tide gauge data and GNSS/levelling point gives consistent separations models between relevant reference levels along the Norwegian coast line
- These separation models make it easier to transform data referring to Sea Chart Datum, NN2000, Mean Sea Level or Euref89 to a common reference level.
- Without a new realization of NN2000 the improved Href (fitted geoid model) can not be taken publicly in use
- The models will be regularly updated when more observations are available
- We are working on uncertainty estimates of the models
- A seamless connection to international altimetry based models, for instance DTU18.