# Satellite Altimetry Based Absolute Dynamic Topography Prediction Using Machine Learning in Baltic Sea

Majid Mostafavi<sup>1</sup>, Nicole Delpeche-Ellmann<sup>2</sup>, Artu Ellmann<sup>1</sup>

<sup>1</sup> Department of Civil Engineering and Architecture, Tallinn University of Technology (majid.mostafavi@taltech.ee), <sup>2</sup> Department of Cybernetics, Tallinn University of Technology

# Introduction

Determining Absolute Dynamic Topography (DT) of the ocean is a key component in examining realistic sea level and for understanding meso-scale dynamics. It is common that tide gauge (TG) data once referred to the geoid can provide high resolution DT estimates however, limited to a fixed location in the coastal areas. Satellite altimetry (SA) provides sea level data along their tracks both at the coast and offshore. Whilst SA has some limitation (e.g., spatial, and temporal limitations, in adequate corrections, land contamination etc.), utilizing high-resolution geoid models allows the determination of a more realistic DT. This study examines different techniques with SA data to predict DT at a temporal resolution of 24 months.

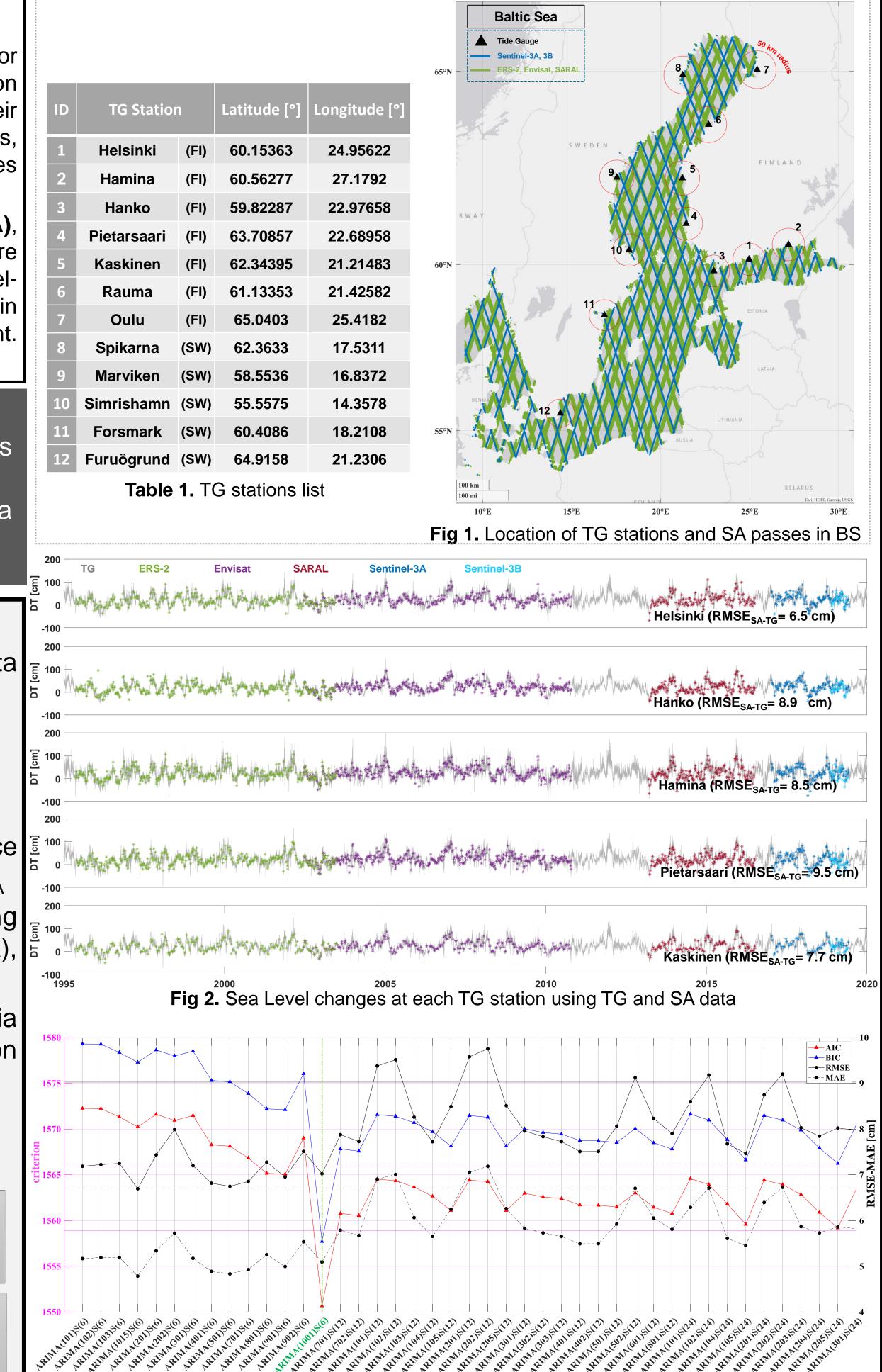
Multiple autoregression methods including Autoregression (AR), Moving Average (MA), Autoregressive Moving Average (ARMA), Autoregressive Integrated Moving-Average (SARIMA) are employed using SA data during 1995-2019 (that includes ERS-2, Envisat, SARAL, Jason-1, Jason-2, CryoSat-2, Jason-3, Sentinel-3A and Sentinel-3B) to predict detrended absolute DT. The predicted SA data are evaluated against the 12 TG stations records in Baltic Sea. The results of this study of a more realistic DT can be applicable for engineering, navigation, and coastal management. Also, careful spatial data selection and outliers' removal using data screening is prerequisite.

# Datasets

**TG:** 12 TG stations data in Baltic Sea (Table 1) **SA:** Sentinel-3A (S3A), Sentinel-3B (S3B), SARAL (SRA), Envisat (ENV), ERS-2 (ER2) data during 1995-2019 using

## Objectives

Detecting most robust model for SA data times series forecasting at vicinity of TG station.
 Sea Level Trend analysis using forecasted SA data



#### ALES+ retracker (Baltic+SEAL) **Model:** NKG2015 Geoid & NKG2016LU Land Uplift

## in the Baltic Sea.

# Methodology

- Spatial selection and outlier detection: extract SA data within 50km from TG and screen out low-quality data using data screening.
- 2. Vertical land movement (VLM) correction for TG time series.
- 3. Bias between SA and TG applied as the difference of mean of each dataset at single TG location.
- 4. Monthly average of SA DT of each mission at near each TG considered as  $DT_{SA}$ .
- Test DT<sub>SA</sub> data stationary using Augmented Dickey-Fuller test. Also, transforming data to 1) detrended: reduce 1<sup>st</sup> degree polynomial trend of DT<sub>SA</sub>, 2) difference: differences between adjacent elements of detrended DT<sub>SA</sub>
- SA DT time series forecasting for 2 years using different models including: Autoregression (AR), Moving Average (MA), Autoregressive Moving Average (ARMA), Autoregressive Integrated Moving Average (ARIMA), Seasonal Autoregressive Integrated Moving-Average (SARIMA).
- Assess model adequacy using Akaike information criteria (AIC) and Bayesian (Schwarz) information criteria (BIC) to select the most robust model also using statistical evaluation criteria, including the correlation coefficient (R), Root Mean Square Error (RMSE) and Mean Absolute Error (MAE):

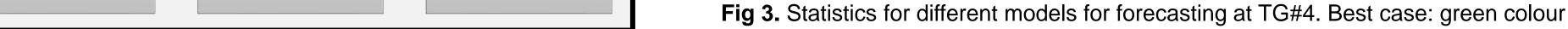
$$R = \begin{bmatrix} \sum_{i=1}^{n} (y_{i}^{0} - \overline{y^{0}})(y_{i}^{r} - \overline{y^{r}}) \\ \sum_{i=1}^{n} (y_{i}^{0} - \overline{y^{0}}) \sum_{i=1}^{n} (y_{i}^{r} - \overline{y^{r}}) \end{bmatrix} RMSE = \sqrt{\frac{1}{n} \sum_{i=1}^{n} (y_{i}^{0} - y_{i}^{r})} MAE = \frac{1}{n} \sum_{i=1}^{n} |y_{i}^{0} - y_{i}^{r}|$$

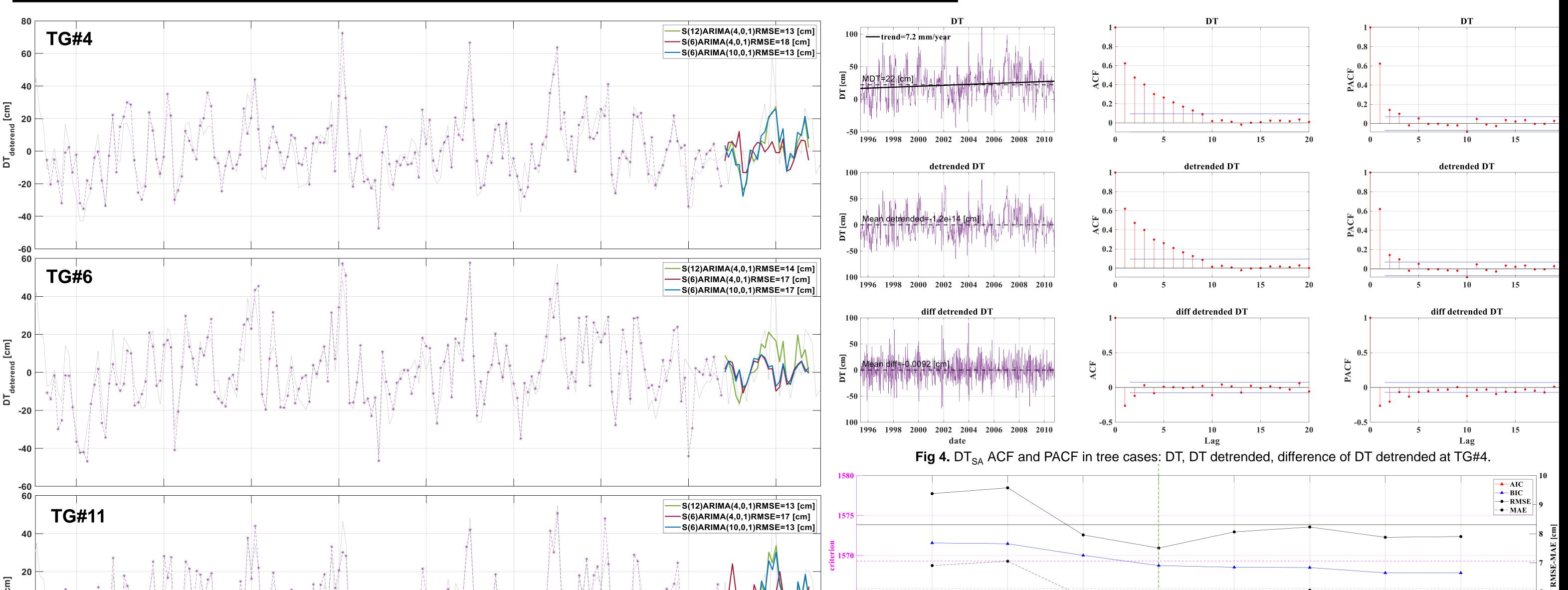
$$MAE = \frac{1}{n} \sum_{i=1}^{n} |y_{i}^{0} - y_{i}^{r}|$$

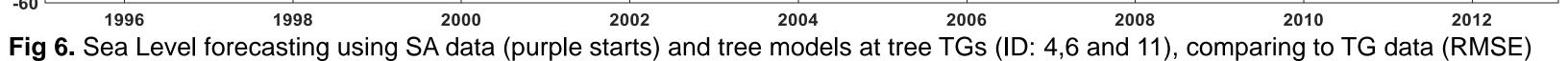
$$MAE = \frac{1}{n} \sum_{i=1}^{n} |y_{i}^{0} - y_{i}^{r}|$$

$$\frac{NAE}{y^{0}} = \frac{1}{y_{i}^{0} - y_{i}^{r}}$$

$$\frac{$$







# Results

- Good agreement is obtainable using SARIMA by ARIMA(4,0,1) SAR(48) SMA (12) with 12 month Seasonality model for DT<sub>SA</sub> forecasting (Figure 3 and 5).
- DT data need to be detrended to consider for Sea Level Trend before forecasting (Figure 4).
- DT forecasting can be forecasted by ~15 cm RMSE using SA data for 2 years. This forecasted data can be served for 2 years data gap of SA data (during 2011-2013).

Nordic Geodetic Commission General Assembly: Planet Ocean and Geodesy 5-8 Sep 2022, Copenhagen, Denmark

ARIMA(1,0,1)S(6) ARIMA(2,0,1)S(6) ARIMA(3,0,1)S(6) ARIMA(4,0,1)S(6) ARIMA(5,0,1)S(6) ARIMA(7,0,1)S(6) ARIMA(8,0,1)S(6) ARIMA(9,0,1)S(6)

Fig 5. SARIMA models of DT<sub>SA</sub> at TG#4 by two different seasonality (6 and 12 month). Best case: green

#### Acknowledgements

The research is supported by the Estonian Research Council grants PRG330 'Development of an iterative approach for near-coast marine geoid modelling by using re-tracked satellite altimetry, in-situ and modelled data'



