



NKG General Assembly, Copenhagen, 2022 Søren Skaarup Larsen, sorla@space.dtu.dk

GNSS based leveling with cm accuracy using TAPAS

The main questions?

- How accurately can we measure height using GNSS-RTK?
- How do we achieve the best accuracy in a reasonable way?
- Can we replace traditional leveling by GNSS?



Oh, wow! You've

grown 0.3 cm since last time



The setup

Aarhus (Red marker) 13 SDFI permanent Gothenburg E39 Baselines shown: 5, 10 and 23km GNSS reference stations Hår (Green markers) Haldum 505 Grundfør Todbjer Kejlstrup Tinning Bronderslev E45 Hinnerup Skødstrup 505 Studstrup Grønfeld Trige Norring Aalborg Vrinners E45 Ē6 505 Ølsted Falkenberg Lystrup Skæring Lisbjerg Lading Egå Knebel Hadsun Bogens O Gedina 511 AARHUS N Mundelstrup Dejret Tved Vistoft 505 E45 Brendstrup Risskov Tillerup Randers jelle Rendborup Eg Strands Herskind True 0 Lyngby Aarhus 195 Brabrand 195 E AARHUS C Kongsgårde Harley Helsingborg Hvide Sand Storring Fejrup Esby Municipality Viby Højbierg Skale Bakker Hasselager Stize Ørby 170 ndsted 433 0 Ma Adslev Skåde 451 511 Tranbjerg Hørning 170 Marslet Mesing 170 Hadersle Beder Stilling E45 Gram E47 Falste ~30 km 0

TAPAS: 11 reference stations (Purple markers)

Solutions made by a monitoring station in central

The monitoring station

- A setup consisting of:
 - 8 Septentrio Mosaic Multifrequency receivers
 - A survey grade multifrequency antenna



- Antenna mounted on top of building, in good open sky conditions
- Network solution provided by the GNSMART software developed by Geo++





Initial investigations

- Which provide the best accuracy?:
 - Network or single station solutions?
 - FKP, VRS or SSR network solutions?
 - What network size/density?
 - What number of satellites / signals / frequencies?
 - What elevation angle?
 - What time of day / year?



Network solutions



TAPAS SSRZ

TAPAS VRS TAPAS FKP



Measurements of height



Note: We will only be taking fixed solution into account.

Solutions of lower quality may occur, but are discarded in our investigation





Solution	Avg. height deviation [cm]	95% interval [cm]
TA11 – default	1.2	1.0
TA11 – 25°	1.7	1.2



Note: The receivers are using a 10 dBHz C/N0 mask





Bias / confidence (95%) [cm]

Solution/Period	1 (March)	2 (March)	3 (April)	4 (May)	5 (June)	6 (July)
TA04 (23km)	2.4/2.0	2.9/1.6	3.0/1.4	3.1/2.4	2.5/2.2	2.5/2.2
TA11 (10km)	1.0/1.2	1.2/1.0	1.6/1.4	1.5/1.6	1.5/1.8	1.4/2.0
TA05 (5km)	1.8/1.0	1.8/1.0	2.1/1.0	2.1/1.2	2.0/1.2	1.9/1.4
TA11+sparse FKP	0.6/1.2		0.5/1.4	0.3/2.0	0.3/1.6	0.2/1.8
TAPAS FKP (3km)	-0.1/0.8	0.4/0.8	0.6/1.0	0.6/1.0	0.7/1.0	0.6/1.2





Distance to the nearest reference station

1 (March)	2 (March)	3 (April)	4 (May)	5 (June)	6 (July)
2.4/2.0	2.9/1.6	3.0/1.4	3.1/2.4	2.5/2.2	2.5/2.2
1.0/1.2	1.2/1.0	1.6/1.4	1.5/1.6	1.5/1.8	1.4/2.0
1.8/1.0	1.8/1.0	2.1/1.0	2.1/1.2	2.0/1.2	1.9/1.4
0.6/1.2		0.5/1.4	0.3/2.0	0.3/1.6	0.2/1.8
-0.1/0.8	0.4/0.8	0.6/1.0	0.6/1.0	0.7/1.0	0.6/1.2
	1 (March) 2.4/2.0 1.0/1.2 1.8/1.0 0.6/1.2 -0.1/0.8	1 (March)2 (March)2.4/2.02.9/1.61.0/1.21.2/1.01.8/1.01.8/1.00.6/1.20.1/0.80.4/0.8	1 (March)2 (March)3 (April)2.4/2.02.9/1.63.0/1.41.0/1.21.2/1.01.6/1.41.8/1.01.8/1.02.1/1.00.6/1.20.5/1.4-0.1/0.80.4/0.80.6/1.0	1 (March)2 (March)3 (April)4 (May)2.4/2.02.9/1.63.0/1.43.1/2.41.0/1.21.2/1.01.6/1.41.5/1.61.8/1.02.1/1.02.1/1.02.1/1.20.6/1.20.5/1.40.3/2.0-0.1/0.80.4/0.80.6/1.00.6/1.0	1 (March)2 (March)3 (April)4 (May)5 (June)2.4/2.02.9/1.63.0/1.43.1/2.42.5/2.21.0/1.21.2/1.01.6/1.41.5/1.61.5/1.81.8/1.01.8/1.02.1/1.02.1/1.22.0/1.20.6/1.20.5/1.40.3/2.00.3/1.6-0.1/0.80.4/0.80.6/1.00.6/1.00.7/1.0

There seems to be a station dependent bias on the single station solutions. We're suspecting this has to do with the antenna handling in the receivers

The distance to the nearest station matters.

Std in general improves with the distance to the reference station.

This goes for both single and network solutions.

Network density mostly matters with regards to reference station redundancy.



Network vs. Single station

Station/Period	1 (March)	2 (March)	3 (April)	4 (May)	5 (June)	6 (July)
TA04 (23km)	2.4/2.0	2.9/1.6	3.0/1.4	3.1/2.4	2.5/2.2	2.5/2.2
TA11 (10km)	1.0/1.2	1.2/1.0	1.6/1.4	1.5/1.6	1.5/1.8	1.4/2.0
TA05 (5km)	1.8/1.0	1.8/1.0	2.1/1.0	2.1/1.2	2.0/1.2	1.9/1.4
TA11+sparse FKP	0.6/1.2		0.5/1.4	0.3/2.0	0.3/1.6	0.2/1.8
TAPAS FKP (3km)	-0.1/0.8	0.4/0.8	0.6/1.0	0.6/1.0	0.7/1.0	0.6/1.2

In general, the network solution performs better on both bias and std

The general downside to the network solution is that in some cases it may end up in a "bad" state. In this case the corrections delivered by the network are of low quality, but will still provide a fixed solution in the receiver -> The user has no way of knowing this.

This leads to decreased accuracy in the height and tends to increase especially the std of the solution.



Network issues

A sparse network with a single TAPAS station



The shortest baseline has now gone from 10 to 80km

Conclusions so far

- Currently we can achieve a solution of the height that's:
 - On average ~5mm off true height
 - Has a 95% confidence of less than ±20mm
- This is achieved by:
 - A sparse network FKP solution
 - Averaging over two shorter periods with a 2 hour gap in between (no correlation)
 - 0 elevation mask on the receiver side (dafault network setup)
 - A nearby reference station at 10km.
 - An antenna with a clear view of the sky
 - A multifrequency, multiconstellation receiver



Future Work

- Look into seasonal and daily variations
- Look into the solution bias (could it be caused by antenna offsets?)

Dad, how tall am

I, then?

• Can we push accuracy even further?

What is the truth?

Well, it's a difficult question, son. 'Cause on average you're 5mm taller when you're in a good mood ets?)