



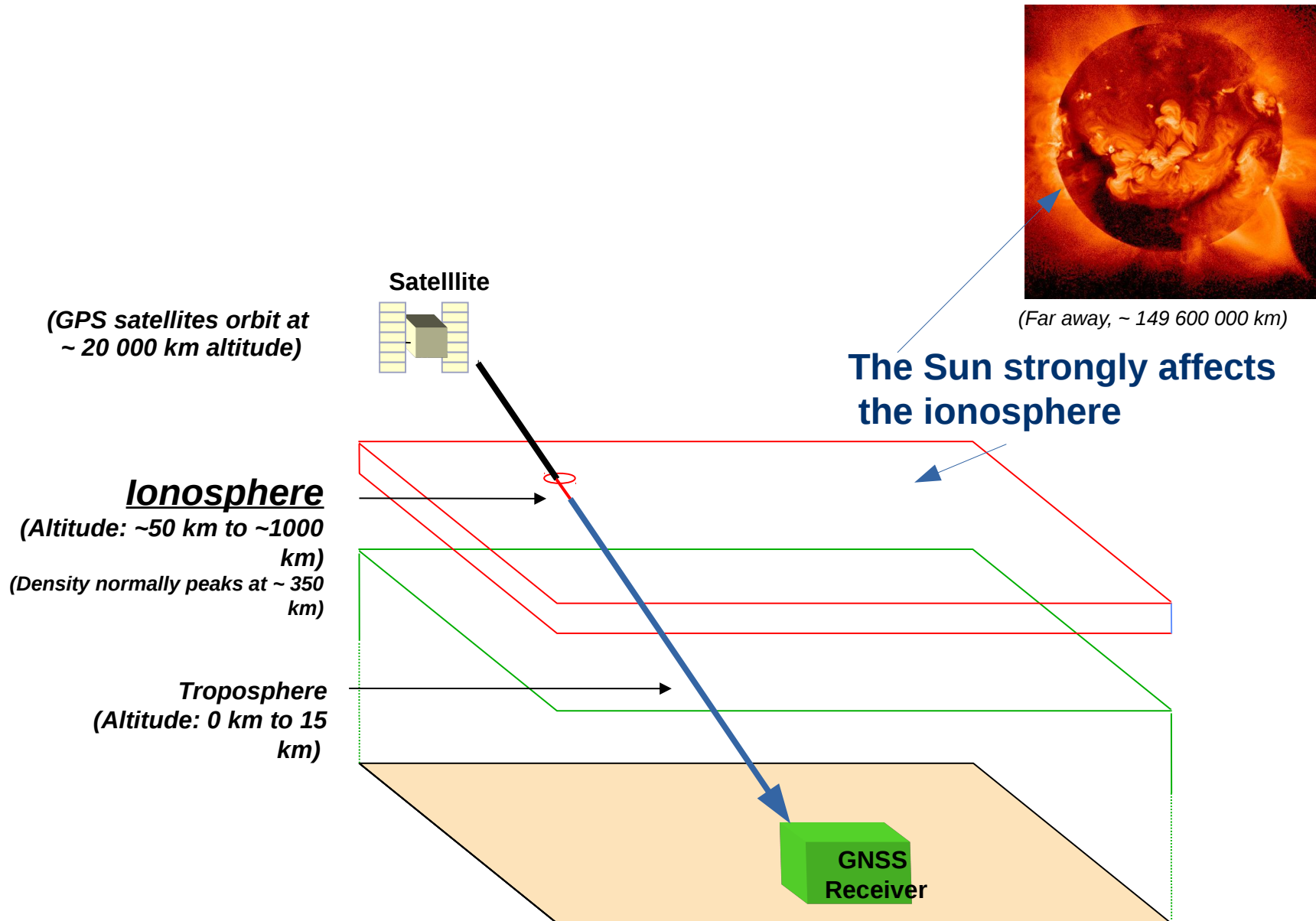
Kartverket

Ionosphere

Part 2 - Effects on GNSS

Knut Stanley Jacobsen

GNSS signals have to pass through the ionosphere



GNSS observation equations

Ideally:

$$\rho_r^s = \sqrt{((x^s - x_r)^2 + (y^s - y_r)^2 + (z^s - z_r)^2)} = ct$$

Range

Satellite "s"

Receiver "r"

Speed of light

Travel time of signal (measured)

GNSS observation equations

Ideally:

$$\rho_r^s = \sqrt{((x^s - x_r)^2 + (y^s - y_r)^2 + (z^s - z_r)^2)} = ct$$

Labels in diagram:
 - Range: points to ρ_r^s
 - Satellite "s": points to x^s, y^s, z^s
 - Receiver "r": points to x_r, y_r, z_r
 - Speed of light: points to c
 - Travel time of signal (measured): points to t

Accounting for various error sources:

$$P_{r,i}^s = \rho_r^s + \delta \rho_r^s + c(\delta t_r - \delta t^s) + T + \frac{1}{f_i^2} I + b_{P,i}^s + b_{r,P,i} + \epsilon_{P_i}$$

Pseudorange

$$L_{r,i}^s = \rho_r^s + \delta \rho_r^s + c(\delta t_r - \delta t^s) + T - \frac{1}{f_i^2} I + b_{L,i}^s + b_{r,L,i} - \lambda_i N_{r,i}^s + \epsilon_{L_i}$$

Phase

Frequency "i"

GNSS observation equations

Ideally:

$$\rho_r^s = \sqrt{((x^s - x_r)^2 + (y^s - y_r)^2 + (z^s - z_r)^2)} = ct$$

Labels for the ideal equation:

- Satellite "s"
- Receiver "r"
- Range
- Speed of light
- Travel time of signal (measured)

Accounting for various error sources:

$$P_{r,i}^s = \rho_r^s + \delta \rho_r^s + c(\delta t_r - \delta t^s) + T + \frac{1}{f_i^2} I + b_{P,i}^s + b_{r,P,i} + \epsilon_{P_i}$$

Labels for the pseudorange equation:

- Satellite orbit error
- Receiver clock error
- Satellite clock error
- Troposphere
- Ionosphere
- Satellite code bias
- Receiver code bias
- Remaining errors (multipath, noise, etc)

Pseudorange

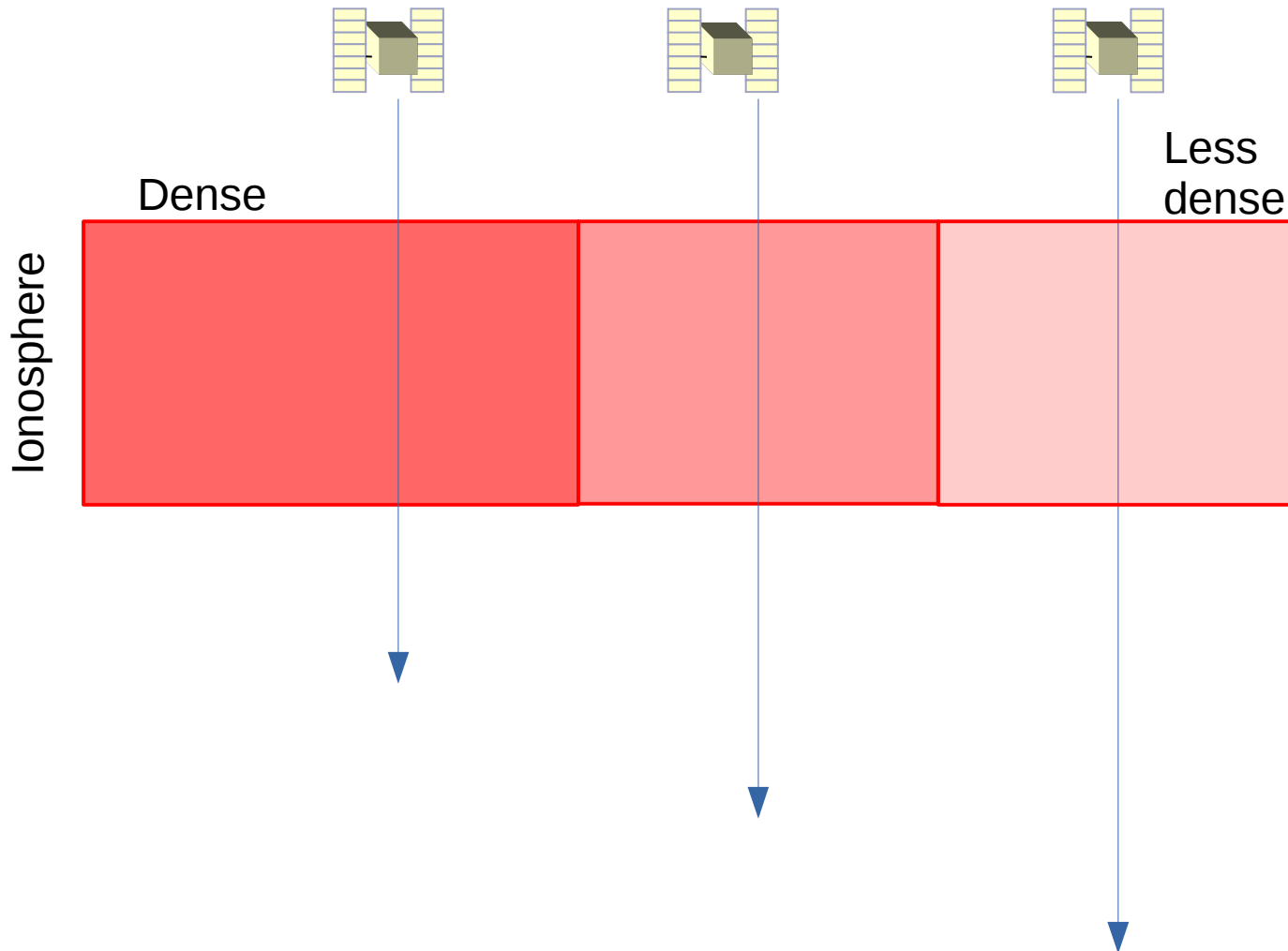
$$L_{r,i}^s = \rho_r^s + \delta \rho_r^s + c(\delta t_r - \delta t^s) + T - \frac{1}{f_i^2} I + b_{L,i}^s + b_{r,L,i} - \lambda_i N_{r,i}^s + \epsilon_{L_i}$$

Phase

Labels for the phase equation:

- Frequency "i"
- Frequency of carrier wave
- Satellite phase bias
- Receiver phase bias
- Wavelength of carrier wave
- Integer ambiguity

Signal delay



Electromagnetic waves are delayed when passing through a plasma.

The delay is proportional to the integrated density of the plasma along the signal path.

In addition, the signal phase is advanced.

Signal delay can be corrected to the first order by the use of dual frequency equipment

Scintillation

Fine structuring of the ionospheric plasma causes random changes to signal phase along the signal wavefront.

The resulting self-interference causes great problems for receivers.

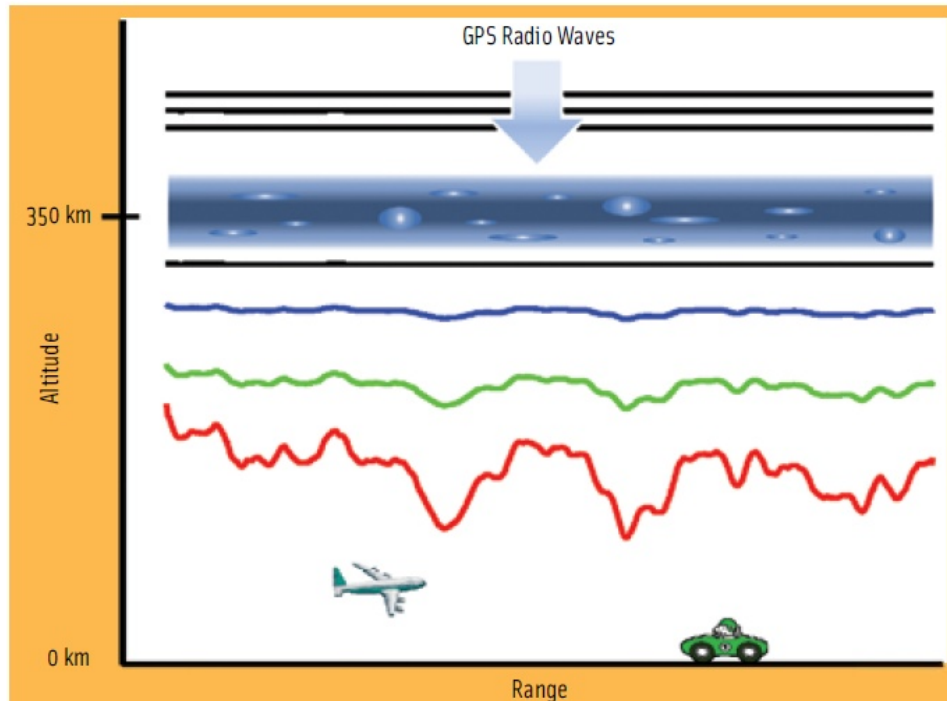


FIGURE 2 Radio wave propagation through a disturbed ionosphere. The horizontal curves represent signal amplitude. Irregularities in the ionosphere introduce phase shifts that become amplitude perturbations as the wave propagates below the ionosphere.

Example: Signal to noise ratios:

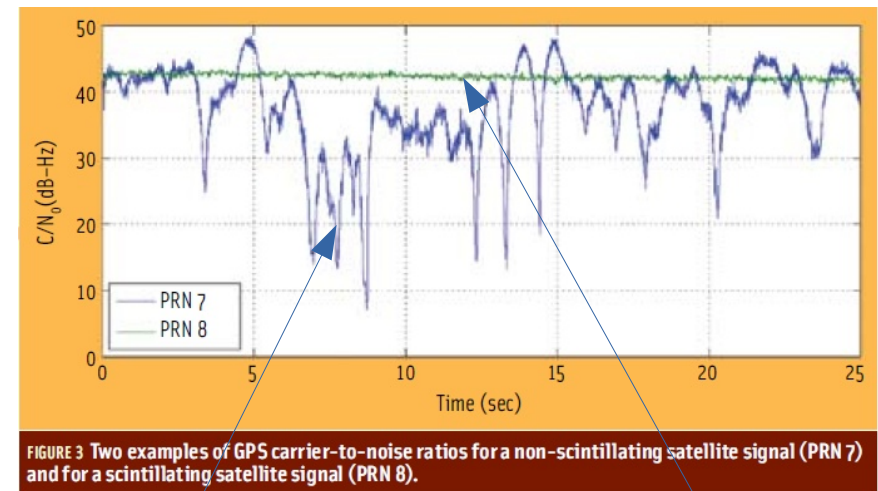


FIGURE 3 Two examples of GPS carrier-to-noise ratios for a non-scintillating satellite signal (PRN 7) and for a scintillating satellite signal (PRN 8).

Blue line:
Disturbed
signal
(scintillation)

Green line:
Undisturbed
signal

Disturbances are quantified by various indices

The amplitude scintillation index “S4” is the normalized standard deviation of the signal intensity

$$S_4 = \frac{\sqrt{\langle I^2 \rangle - \langle I \rangle^2}}{\langle I \rangle^2}$$

The phase scintillation index “sigma phi” is the standard deviation of the detrended signal phase

$$\sigma_\varphi = \sqrt{\langle \varphi^2 \rangle - \langle \varphi \rangle^2}$$

The Rate-Of-TEC-Index (ROTI) is also a measure of phase variation, but through a different equation

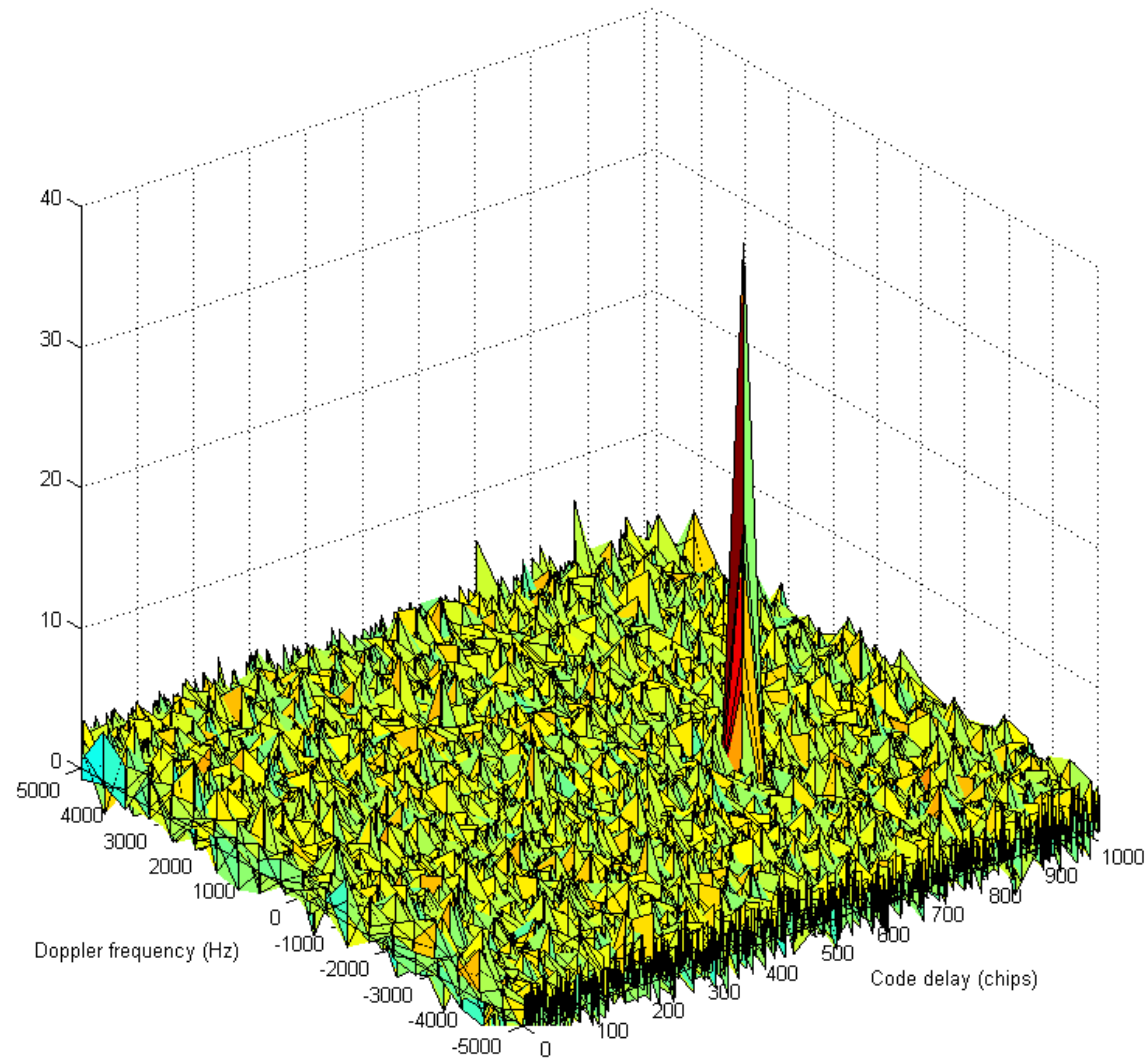
$$ROTI = \sqrt{\langle ROT^2 \rangle - \langle ROT \rangle^2}$$

$$ROT(i) = \frac{L_{GF}(i) - L_{GF}(i-1)}{t(i) - t(i-1)}$$

$$L_{GF}(i) = \lambda_1 L_1(i) - \lambda_2 L_2(i)$$

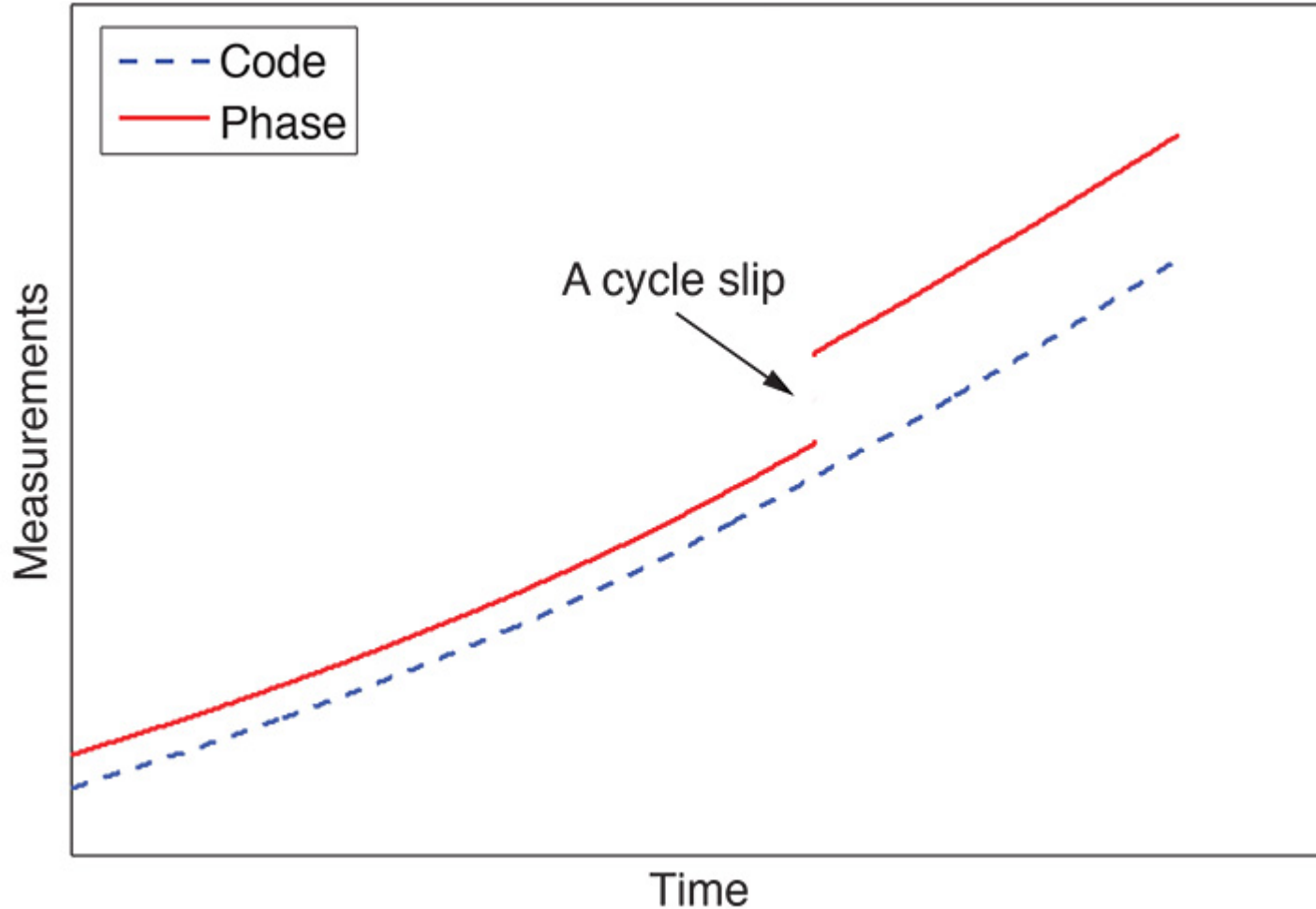
Effects on the receiver hardware

Amplitude and phase scintillations can cause the receiver to lose track of the signal.



Effects on the receiver hardware

Phase scintillations that do not cause a complete tracking loss can cause a partial tracking loss resulting in a break in the phase time series. (a “cycle slip”)



Where do the effects enter the observation equation?

$$P_{r,i}^s = \rho_r^s + \delta \rho_r^s + c(\delta t_r - \delta t^s) + T \boxed{+\frac{1}{f_i^2} I} + b_{P,i}^s + b_{r,P,i} + \epsilon_{P_i}$$

Signal delay

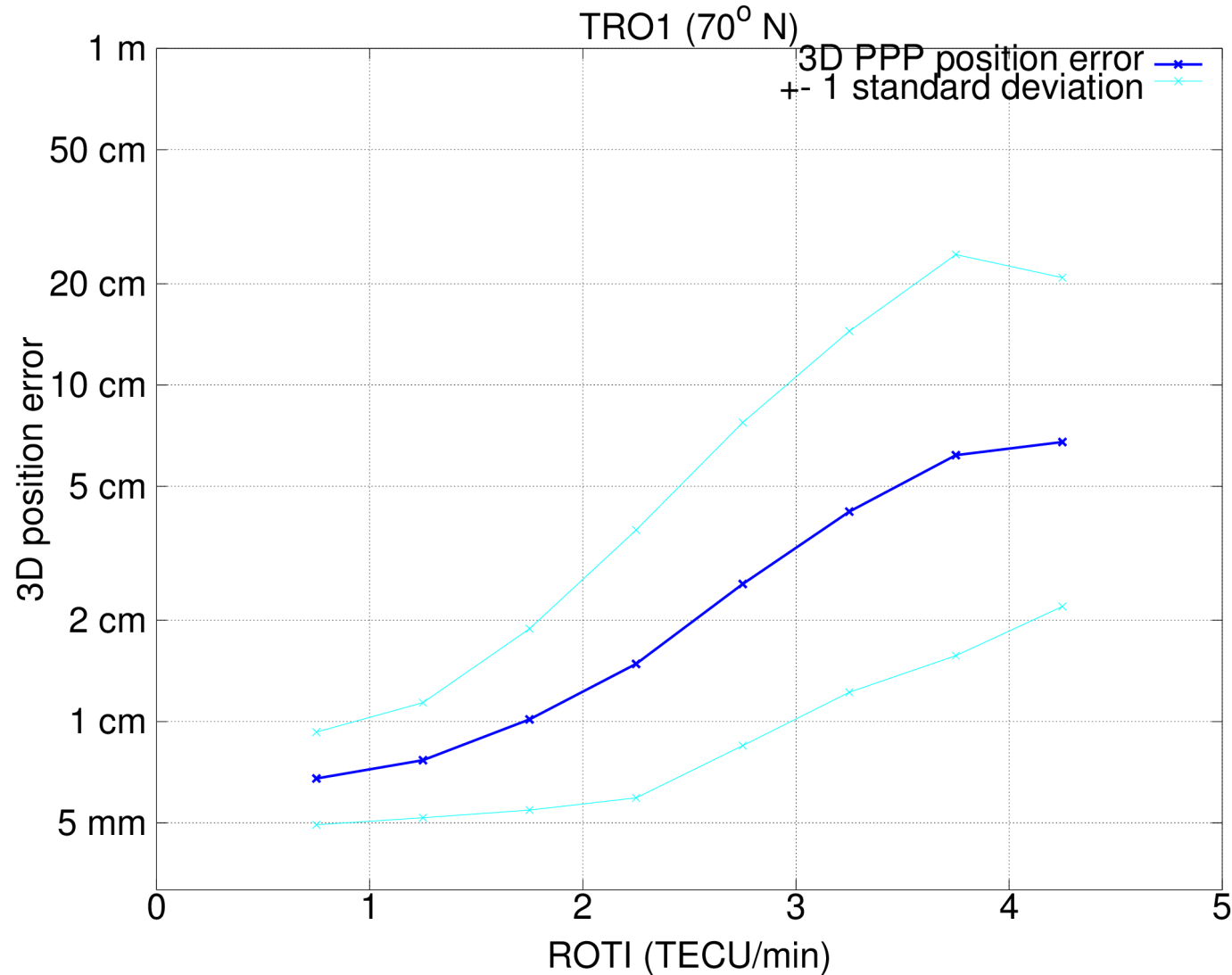
$$L_{r,i}^s = \rho_r^s + \delta \rho_r^s + c(\delta t_r - \delta t^s) + T \boxed{-\frac{1}{f_i^2} I} + b_{L,i}^s + b_{r,L,i} - \lambda_i N_{r,i}^s \boxed{+\epsilon_{L_i}}$$

Phase advance

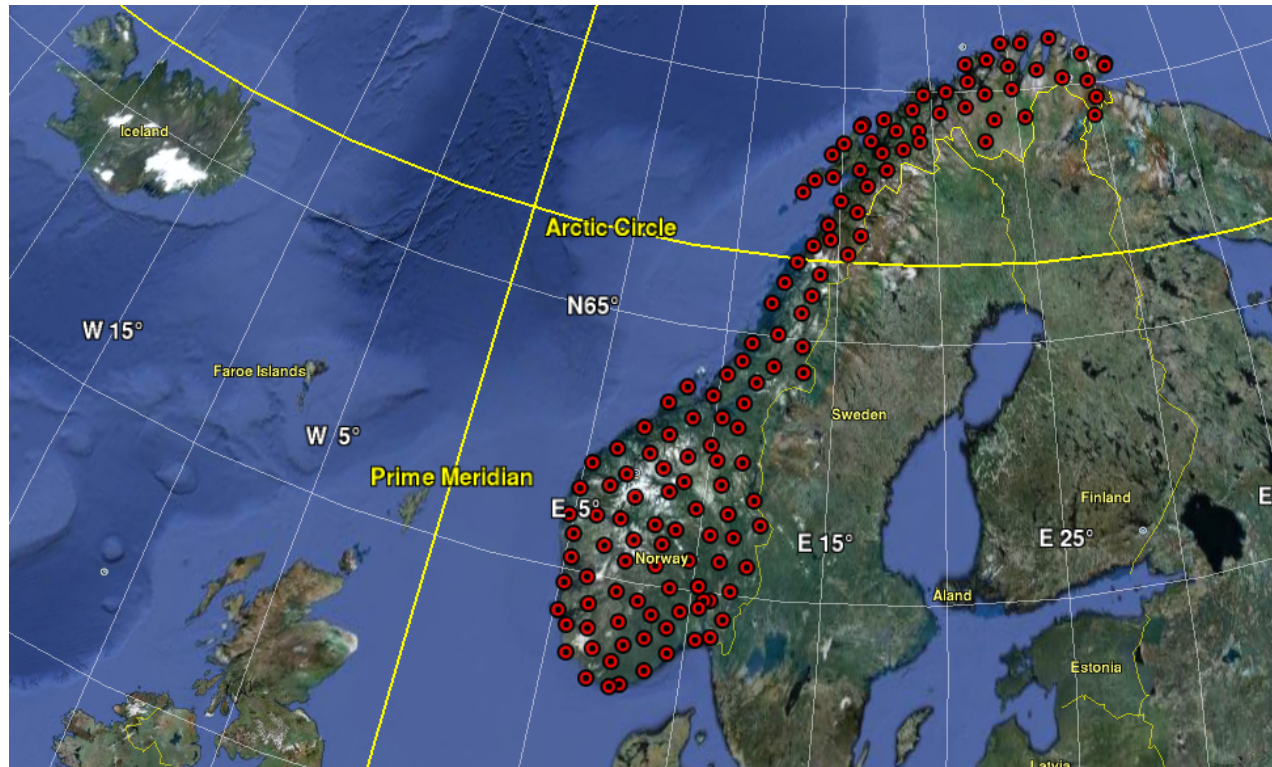
Phase scintillation

(Amplitude scintillation does not enter the observation equation)

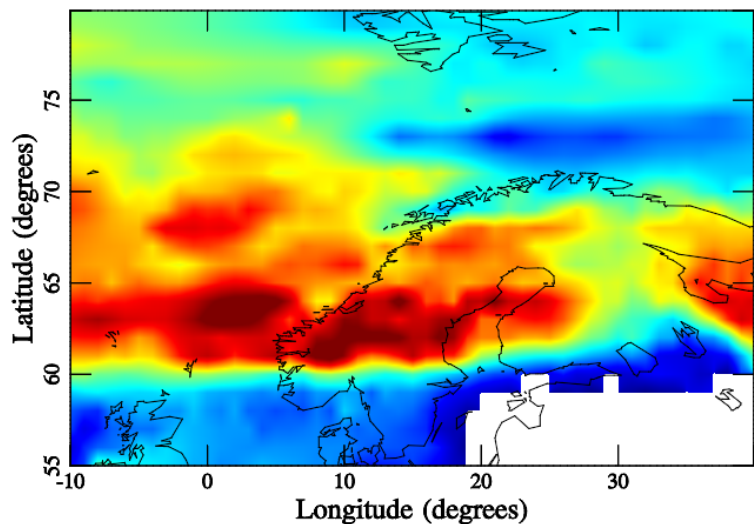
Effects on the position solution



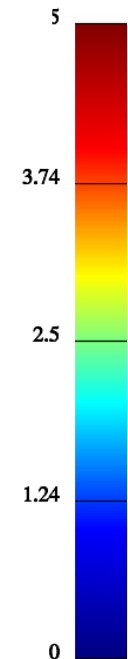
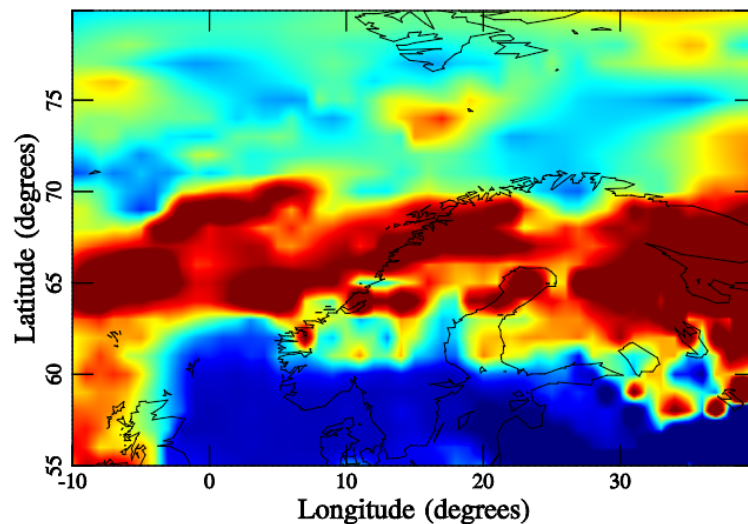
Effects on RTK positioning network



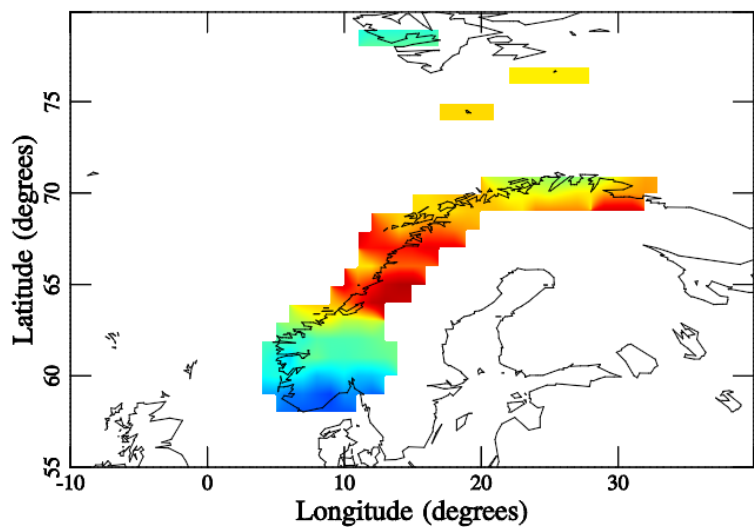
**Amount of plasma in the ionosphere
(TEC)**



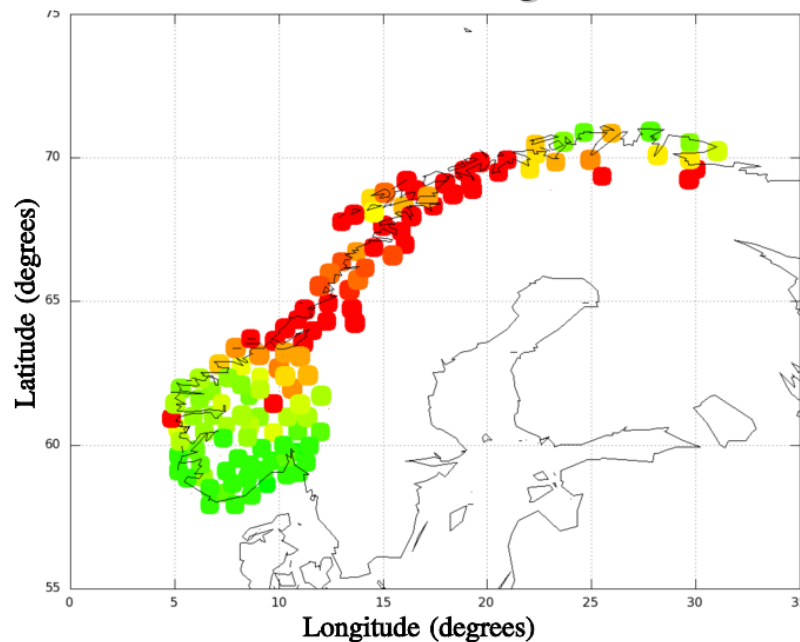
**Ionospheric disturbance level
(ROTI)**



**Effect of disturbances at ground level
(ROTI)**

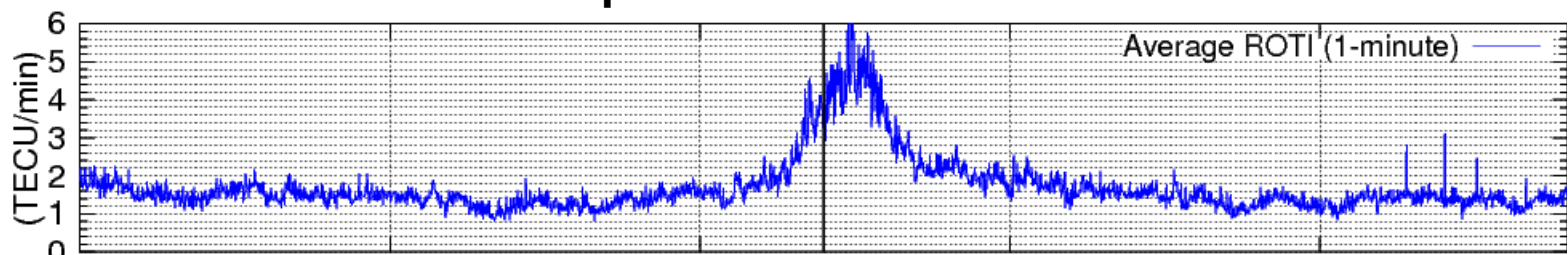


CPOS Processing Status

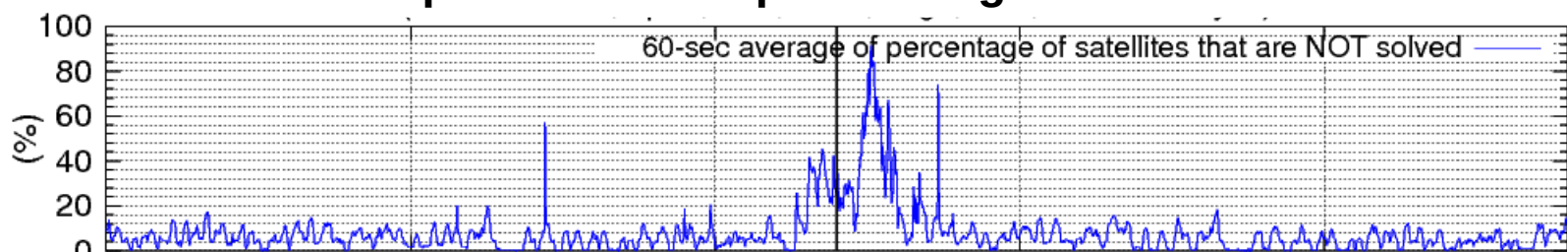


GNSS monitor measures user experience

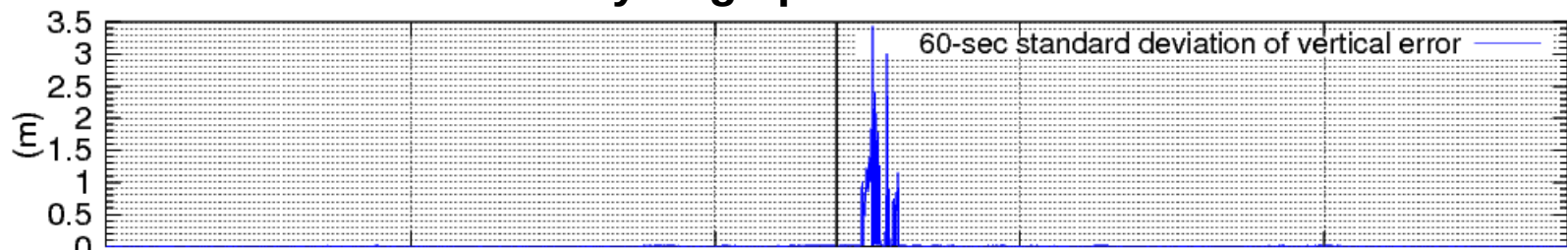
Ionospheric disturbance level



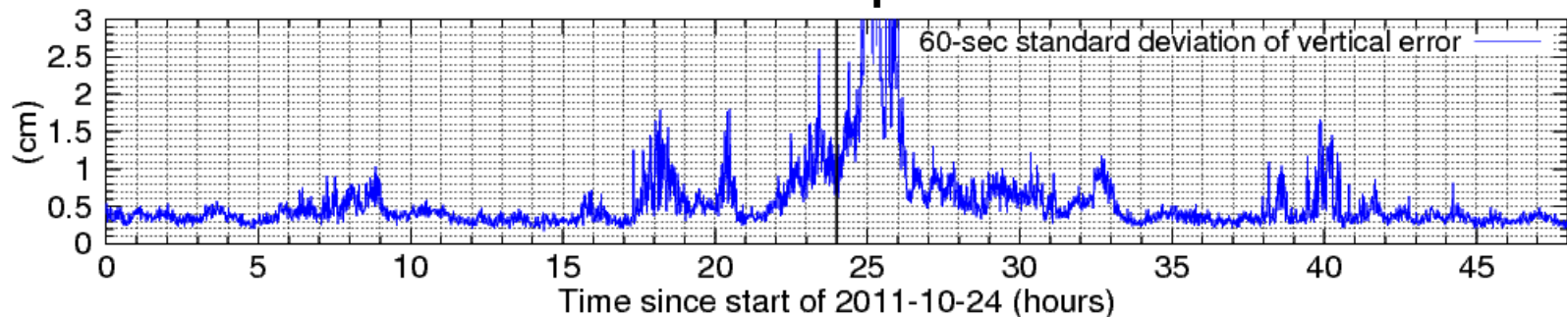
Disruption of CPOS processing near Hønefoss



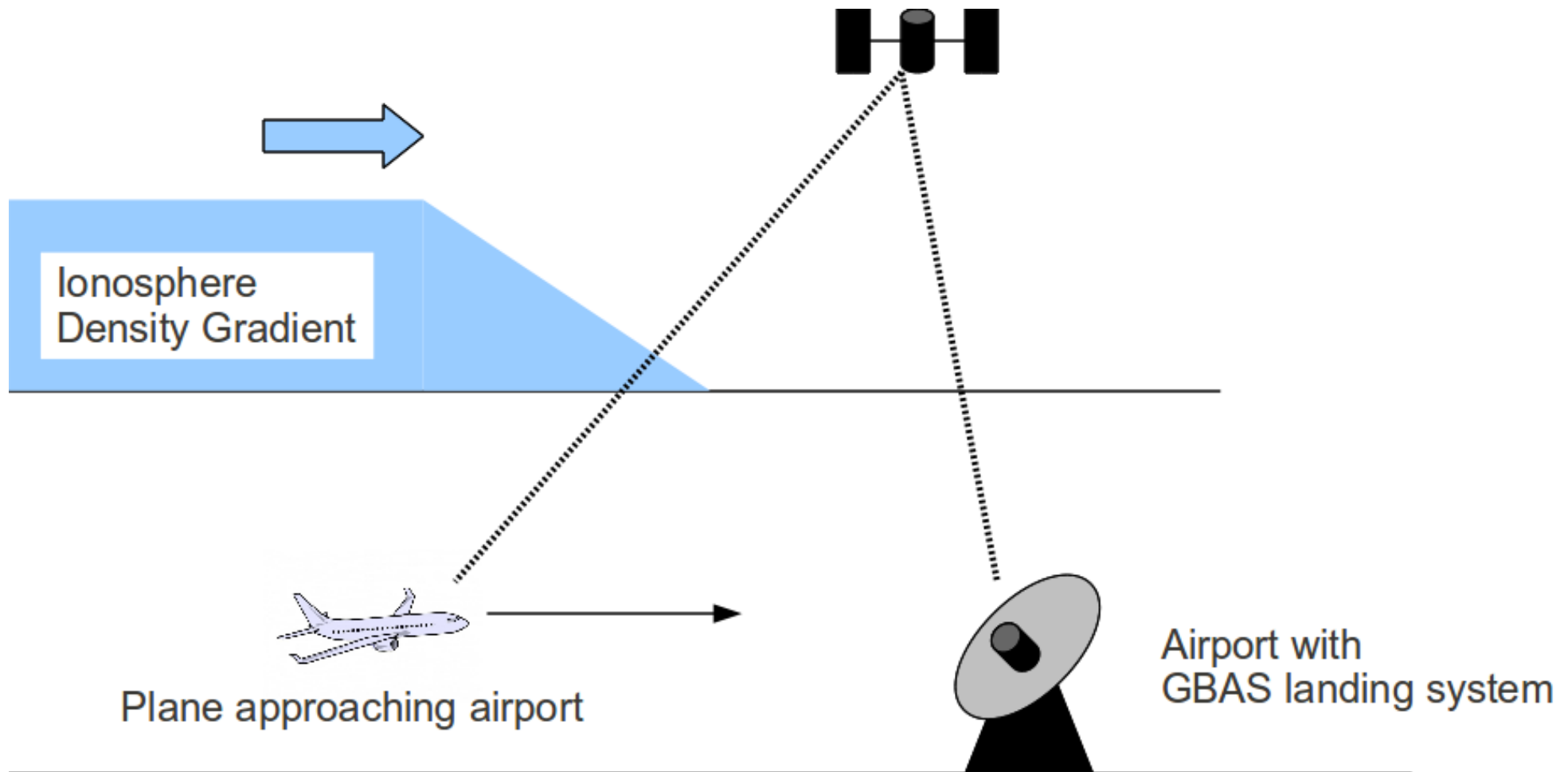
Very large position errors



Small to moderate position errors



Ionospheric gradients may threaten GNSS support systems



Effects on EGNOS

23 October

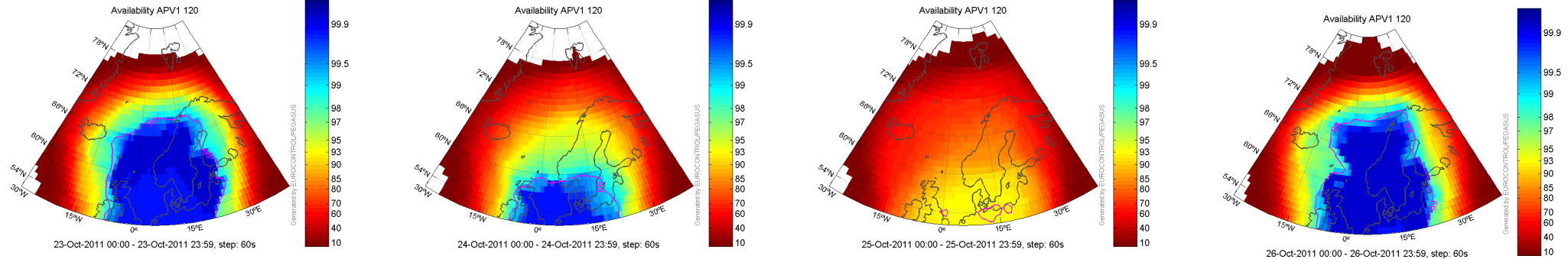
24 October

25 October

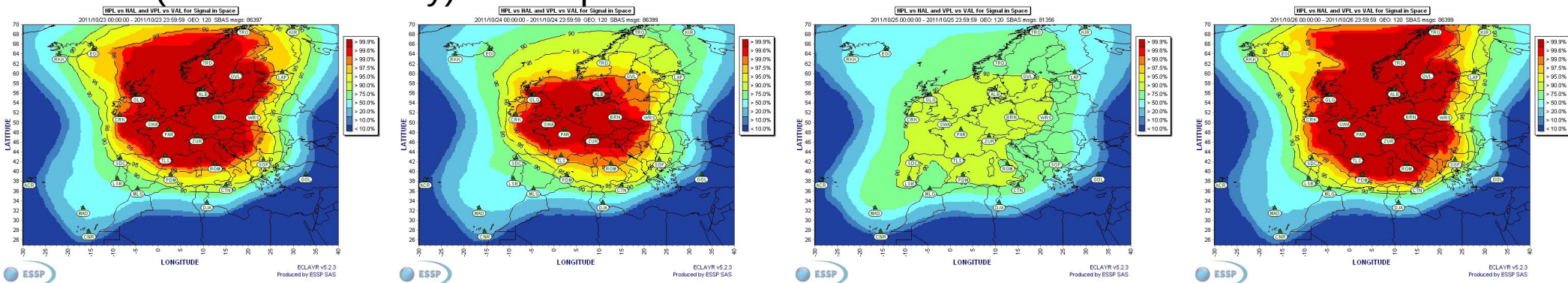
26 October

Geomagnetic storm

EGNOS (APV-1 Availability) in Scandinavia



EGNOS (APV-1 Availability) in Europe



Mitigation - Delay

Signal delay (and phase advance) can be mitigated by:

- Forming a combination of measurements on two frequencies in such a way that the ionospheric component is eliminated

$$P_{r,i}^s = \rho_r^s + \delta \rho_r^s + c(\delta t_r - \delta t^s) + T + \frac{1}{f_i^2} I + b_{P,i}^s + b_{r,P,i} + \epsilon_{P_i}$$

$$L_{r,i}^s = \rho_r^s + \delta \rho_r^s + c(\delta t_r - \delta t^s) + T - \frac{1}{f_i^2} I + b_{L,i}^s + b_{r,L,i} - \lambda_i N_{r,i}^s + \epsilon_{L_i}$$

$$P_{IF} = \frac{f_1^2 P_1 - f_2^2 P_2}{f_1^2 - f_2^2} = \rho_r^s + \delta \rho_r^s + c(\delta t_r - \delta t^s) + T + \frac{f_1^2(b_{P,1}^s + b_{r,P,1}) - f_2^2(b_{P,2}^s + b_{r,P,2})}{f_1^2 - f_2^2} + \frac{f_1^2 \epsilon_{P_1} - f_2^2 \epsilon_{P_2}}{f_1^2 - f_2^2}$$

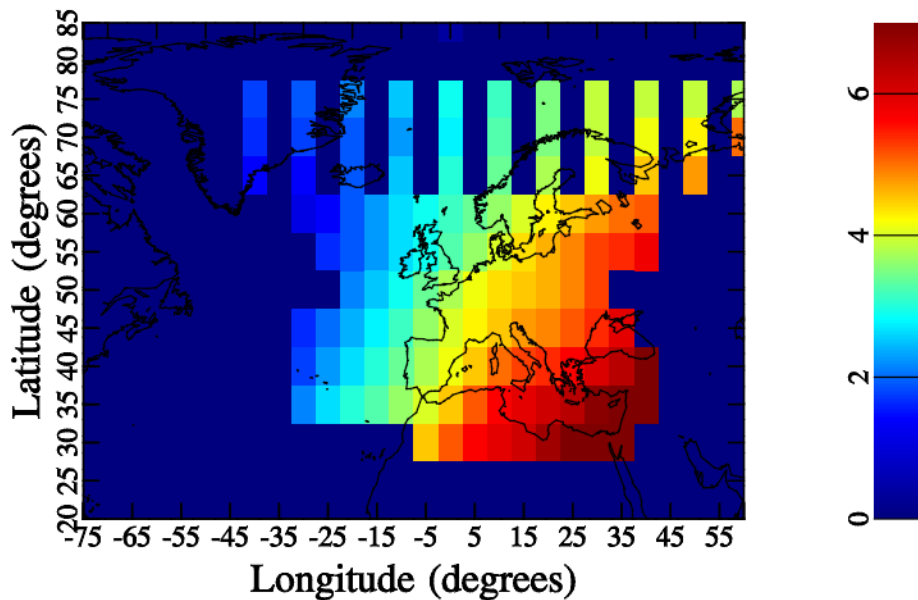
$$L_{IF} = \frac{f_1^2 L_1 - f_2^2 L_2}{f_1^2 - f_2^2} = \rho_r^s + \delta \rho_r^s + c(\delta t_r - \delta t^s) + T + \frac{f_1^2(b_{L,1}^s + b_{r,L,1} - \lambda_1 N_{r,1}^s) - f_2^2(b_{L,2}^s + b_{r,L,2} - \lambda_2 N_{r,2}^s)}{f_1^2 - f_2^2} + \frac{f_1^2 \epsilon_{L_1} - f_2^2 \epsilon_{L_2}}{f_1^2 - f_2^2}$$

Mitigation - Delay

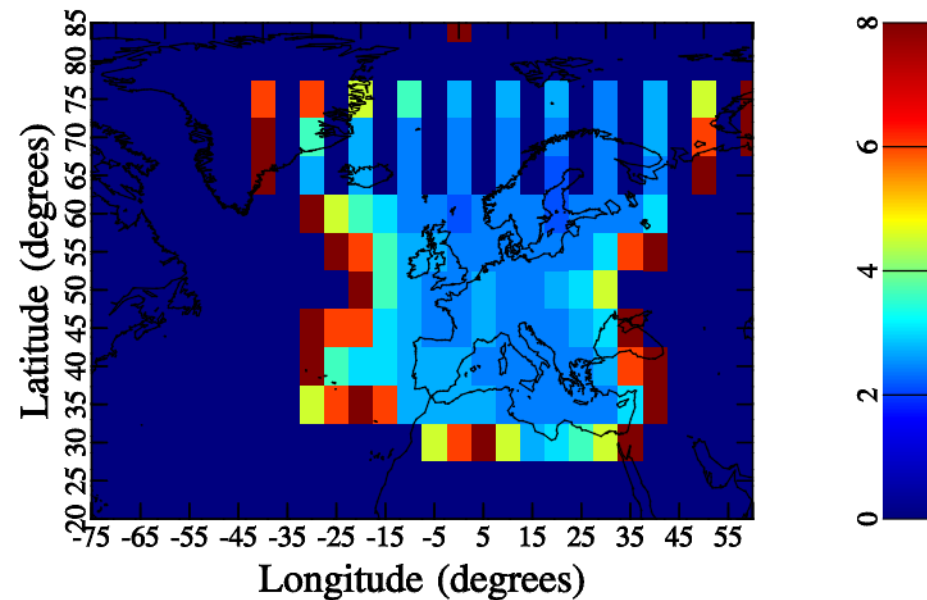
Signal delay (and phase advance) can be mitigated by:

- Receiving information about the ionospheric component from an external source. e.g:
 - Static empirical model
 - Empirical model with measured input variables
 - Measured ionosphere state from a receiver network

Total Electron Content [Meter]
2014-02-25 08:45 UTC



Grid Ionospheric Vertical Error [Meter]
2014-02-25 08:45 UTC



Mitigation - Scintillation

Scintillation is harder to mitigate, and has to be dealt with before the observables (pseudo-range and phase) are formed.

This means that the receiver hardware (and/or software, in the case of a software receiver) has to be built to be robust against scintillation.

Unfortunately, making the hardware robust against scintillation will generally require a decrease in performance in some other fashion.

Example: Normal receivers can handle phase scintillation better by increasing the bandwidth of the phase tracking loop, but this increases the noise in the resulting phase observable.

Question time!

